

# Supplementary Information for: A Model-Based Approach for Pulse Selection from Electrodermal Activity

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## RESULTS ON SIMULATED EDA DATA

TABLE S-I  
RESULTS OF 50 RUNS OF OUR FRAMEWORK ON SIMULATED EDA DATA

Run #	Noise Level	Mu	Lambda	# Pulses (true)	Final Thresh	# Pulses (extracted)	# Pulses matched	Recall	Precision	Est. mu (99% CI)	Est. lambda (99% CI)
1	1e-2	20	8	161	0.025	160	157	0.975	0.981	22.397 ± 7.279	8.821 ± 2.544
2	1e-2	20	8	159	0.023	151	148	0.931	0.980	23.810 ± 7.790	9.805 ± 2.911
3	1e-2	20	8	206	0.023	196	194	0.942	0.990	18.327 ± 4.762	9.218 ± 2.402
4	1e-2	20	8	231	0.022	228	224	0.970	0.983	15.548 ± 3.260*	10.320 ± 2.494
5	1e-2	20	8	184	0.025	183	181	0.984	0.989	19.705 ± 5.427	9.451 ± 2.549
6	1e-2	20	10	180	0.023	176	173	0.961	0.983	20.450 ± 5.737	9.826 ± 2.702
7	1e-2	20	10	170	0.035	168	167	0.982	0.994	21.261 ± 6.062	10.363 ± 2.917
8	1e-2	20	10	216	0.05	208	206	0.954	0.990	17.197 ± 3.592	12.611 ± 3.190
9	1e-2	20	10	183	0.03	177	177	0.967	1.00	20.353 ± 5.158	11.916 ± 3.268
10	1e-2	20	10	163	0.022	163	161	0.988	0.988	22.011 ± 5.849	12.728 ± 3.637
11	1e-2	15	5	279	0.021	249	244	0.875	0.980	14.399 ± 3.350	7.111 ± 1.644*
12	1e-2	15	5	260	0.022	232	228	0.877	0.983	15.543 ± 3.700	7.869 ± 1.885*
13	1e-2	15	5	237	0.019	225	208	0.878	0.924	16.004 ± 3.933	7.840 ± 1.907*
14	1e-2	15	5	255	0.022	237	232	0.910	0.979	15.170 ± 3.656	7.337 ± 1.739*
15	1e-2	15	5	261	0.022	246	241	0.923	0.980	14.570 ± 3.515	6.774 ± 1.576*
16	1e-2	20	5	164	0.021	152	145	0.884	0.954	23.385 ± 8.106	8.522 ± 2.522*
17	1e-2	20	5	203	0.02	186	175	0.862	0.941	19.057 ± 5.450	8.340 ± 2.231*
18	1e-2	20	5	172	0.025	154	151	0.878	0.981	23.177 ± 7.501	9.563 ± 2.812*
19	1e-2	20	5	161	0.023	153	148	0.919	0.967	23.478 ± 8.188	8.398 ± 2.477*
20	1e-2	20	5	216	0.023	198	195	0.903	0.985	18.127 ± 5.185	7.449 ± 1.932*
21	1e-2	30	15	109	0.03	110	109	1.00	0.991	32.531 ± 11.329	16.230 ± 5.646
22	1e-2	30	15	154	0.065	152	151	0.981	0.993	23.054 ± 6.157*	14.155 ± 4.189
23	1e-2	30	15	108	0.045	107	107	0.991	1.00	33.629 ± 13.602	12.788 ± 4.511
24	1e-2	30	15	131	0.025	131	128	0.977	0.977	27.274 ± 8.587	13.981 ± 4.457
25	1e-2	30	15	129	0.06	127	127	0.985	1.00	26.862 ± 7.138	19.940 ± 6.456
26	1e-2	25	10	150	0.024	149	148	0.987	0.993	23.788 ± 7.409	10.954 ± 3.274
27	1e-2	25	10	142	0.065	139	138	0.972	0.993	25.971 ± 8.548	11.480 ± 3.553
28	1e-2	25	10	123	0.03	119	118	0.959	0.992	30.229 ± 11.153	12.422 ± 4.155
29	1e-2	25	10	135	0.03	134	133	0.985	0.993	25.777 ± 8.473	11.851 ± 3.735
30	1e-2	25	10	141	0.03	139	137	0.972	0.986	25.980 ± 8.747	10.976 ± 3.397
31	5e-3	25	10	156	0.011	158	149	0.955	0.943	22.499 ± 7.246	9.138 ± 2.653
32	5e-3	25	10	158	0.08	142	142	0.899	1.00	25.481 ± 7.049	15.608 ± 4.779*
33	5e-3	25	10	138	0.012	140	136	0.986	0.971	25.679 ± 9.649	8.648 ± 2.667
34	5e-3	25	10	135	0.075	123	122	0.904	0.992	28.442 ± 9.495	13.812 ± 4.544
35	5e-3	25	10	153	0.065	143	143	0.935	1.00	24.936 ± 6.969	14.859 ± 4.534*
36	5e-3	15	10	266	0.018	260	260	0.977	1.00	13.866 ± 2.424	11.619 ± 2.629
37	5e-3	15	10	231	0.012	234	229	0.991	0.979	15.321 ± 3.055	10.958 ± 2.614
38	5e-3	15	10	211	0.018	208	206	0.976	0.990	17.345 ± 3.991	10.486 ± 2.653
39	5e-3	15	10	216	0.04	207	207	0.958	1.00	17.252 ± 3.379	14.458 ± 3.667*
40	5e-3	15	10	213	0.014	212	206	0.967	0.972	16.860 ± 3.727	10.835 ± 2.715

41	3e-2	20	12	165	0.065	159	155	0.939	0.975	22.300 + 5.481	15.454 + 4.472
42	3e-2	20	12	190	0.06	191	186	0.979	0.974	18.530 + 3.796	15.387 + 4.062
43	3e-2	20	12	192	0.07	186	182	0.948	0.979	19.219 + 4.239	14.135 + 3.782
44	3e-2	20	12	164	0.135	156	155	0.945	0.994	23.034 + 5.670	16.222 + 4.739
45	3e-2	20	12	146	0.085	135	133	0.911	0.985	25.680 + 7.102	16.555 + 5.199
46	3e-2	25	15	140	0.06	155	138	0.986	0.890	22.759 + 5.098	19.482 + 5.710
47	3e-2	25	15	128	0.08	124	122	0.953	0.984	28.129 + 8.017	18.590 + 6.091
48	3e-2	25	15	144	0.075	146	144	1.00	0.986	24.598 + 6.917	14.183 + 4.283
49	3e-2	25	15	141	0.065	140	138	0.979	0.986	25.655 + 6.598	18.443 + 5.687
50	3e-2	25	15	119	0.075	117	117	0.983	1.00	30.570 + 10.648	14.334 + 4.835

# = number, Noise level = Standard deviation of noise, Mu = scale parameter of inverse Gaussian distribution, Lambda = shape parameter of inverse Gaussian distribution, # Pulses (true) = number of true pulses, Final thresh = final prominence threshold used, # Pulses extracted = number of pulses extracted by our framework, # Pulses matched = number of pulses matched in time between the true and extracted pulses, Recall = proportion of true pulses that were extracted by our framework, Precision = proportion of pulses extracted by our framework that were true pulses, Est. mu (99% CI) = estimated value of scale parameter of inverse Gaussian distribution reported as a 99% confidence interval, Est. lambda (99% CI) = estimated value of shape parameter of inverse Gaussian reported as a 99% confidence interval, \* indicates that the true parameter value was not captured within the 99% confidence interval for that run

TABLE S-II  
SUMMARY OF 50 RUNS OF OUR FRAMEWORK ON SIMULATED EDA DATA BY NOISE LEVEL

Noise Level	Final Thresh (95% CI)	Recall (95% CI)	Precision (95% CI)
1e-2	0.030 + 0.005	0.946 + 0.016	0.982 + 0.006
5e-3	0.035 + 0.018	0.955 + 0.020	0.985 + 0.012
3e-2	0.077 + 0.014	0.962 + 0.017	0.975 + 0.019
Overall	0.040 + 0.007	0.951 + 0.011	0.981 + 0.006

Noise level = Standard deviation of noise, Final thresh (95% CI) = final prominence threshold used reported as a 95% confidence interval, Sensitivity (95% CI) = proportion of true pulses that were extracted by our framework reported as a 95% confidence interval, Positive predictive value (95% CI) = proportion of pulses extracted by our framework that were true pulses reported as a 95% confidence interval

## AWAKE AND AT REST COHORT

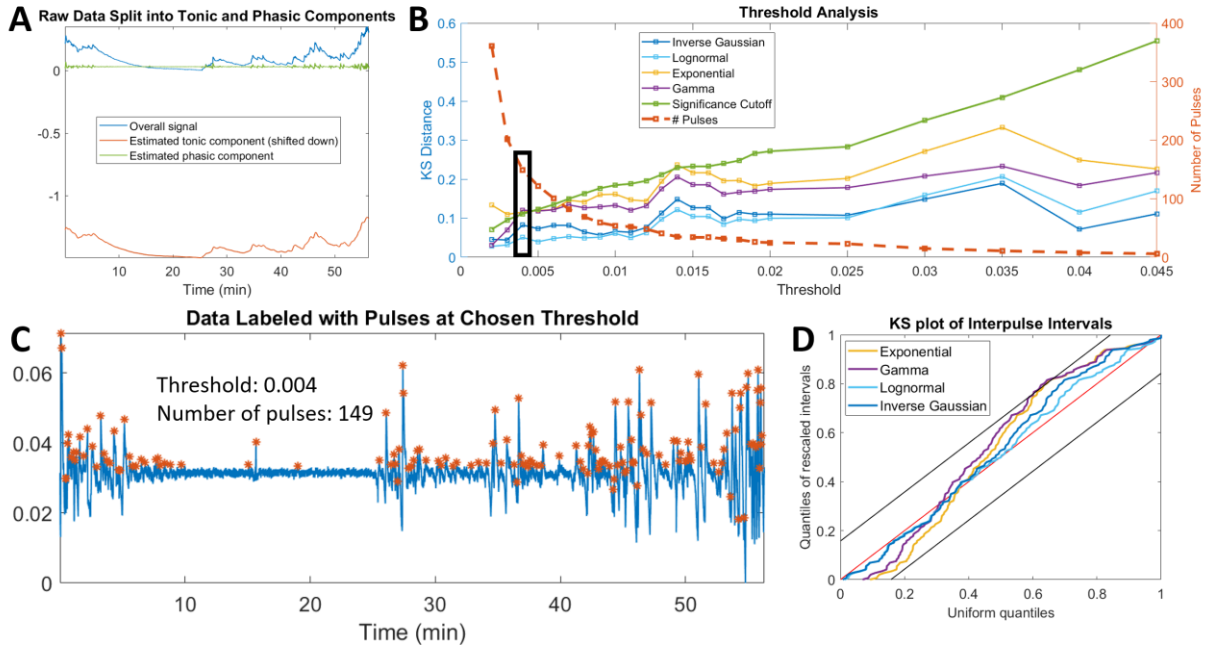


Fig. S1. Results for Subject S1 from the awake and at rest cohort, showing agreement with the trends of the cohort as a whole. (a) Preprocessing of data by splitting into tonic and phasic components, (b) Screening of thresholds with chosen threshold marked with bolded rectangle, (c) Pulses extracted at chosen threshold, (d) Full KS-plot showing goodness-of-fit at chosen threshold

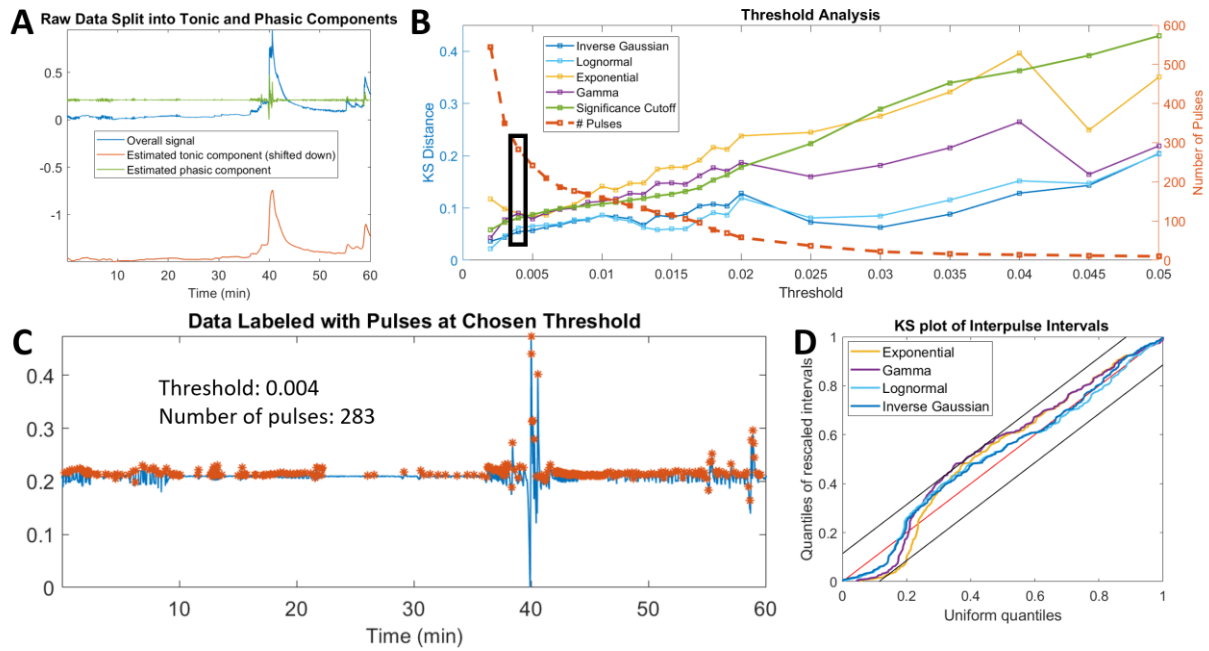


Fig. S2. Results for Subject S2 from the awake and at rest cohort, showing agreement with the trends of the cohort as a whole. (a) Preprocessing of data by splitting into tonic and phasic components, (b) Screening of thresholds with chosen threshold marked with bolded rectangle, (c) Pulses extracted at chosen threshold, (d) Full KS-plot showing goodness-of-fit at chosen threshold

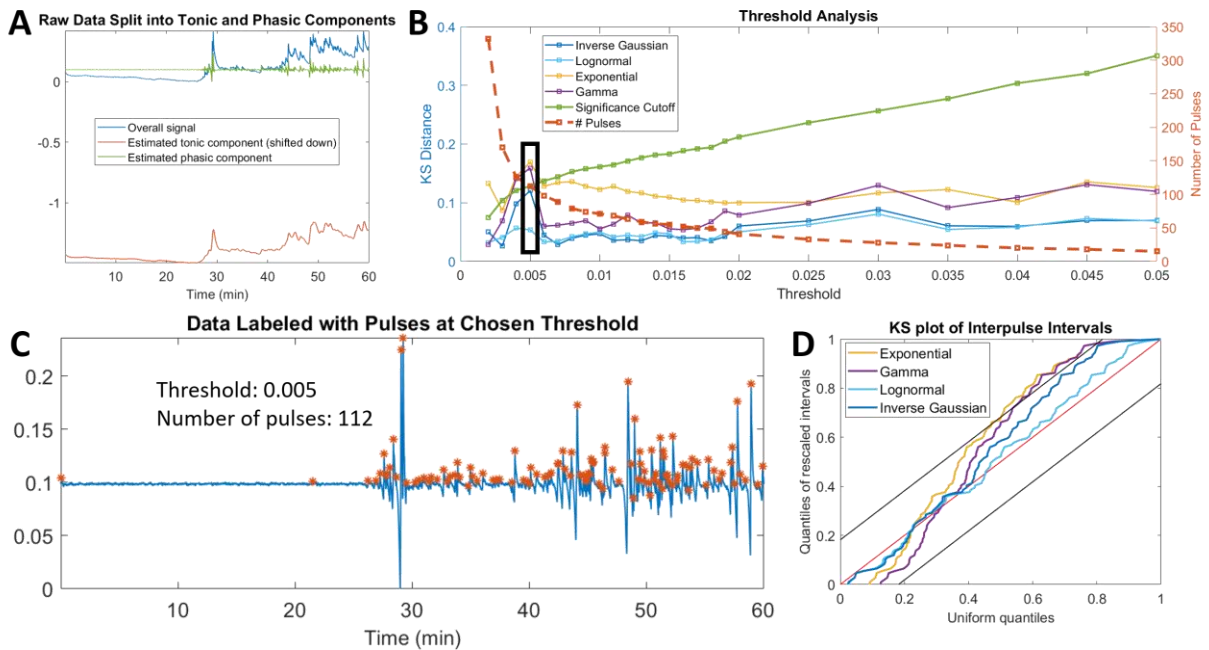


Fig. S3. Results for Subject S3 from the awake and at rest cohort, showing agreement with the trends of the cohort as a whole. (a) Preprocessing of data by splitting into tonic and phasic components, (b) Screening of thresholds with chosen threshold marked with bolded rectangle, (c) Pulses extracted at chosen threshold, (d) Full KS-plot showing goodness-of-fit at chosen threshold

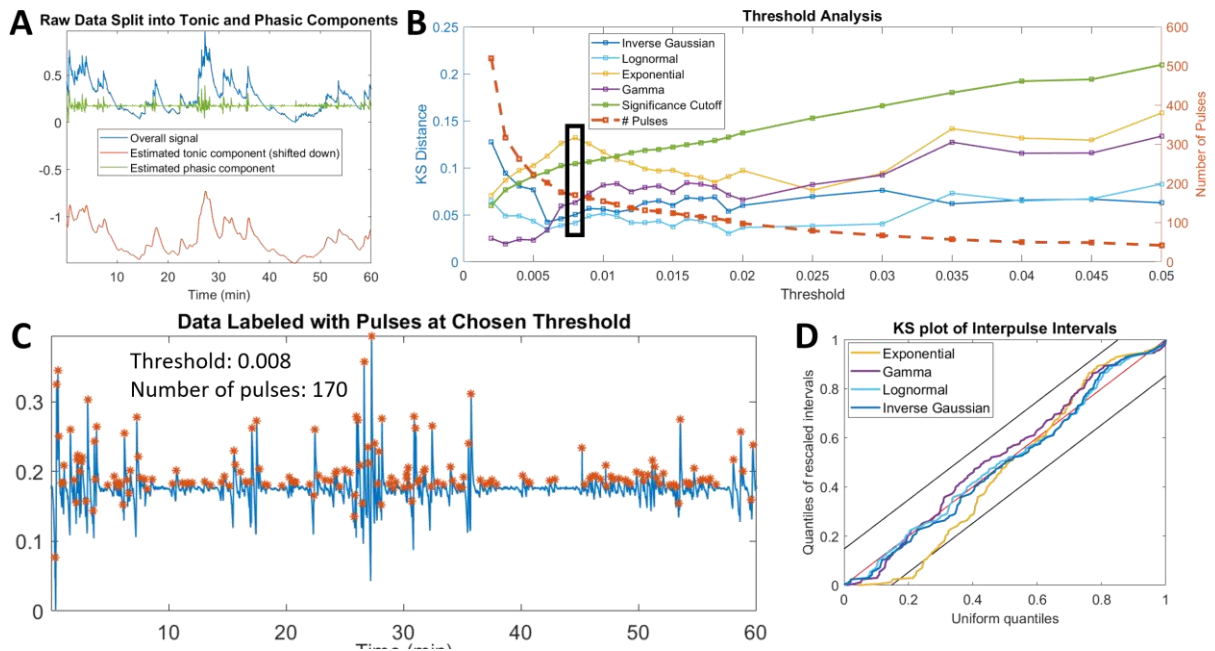


Fig. S4. Results for Subject S4 from the awake and at rest cohort, showing agreement with the trends of the cohort as a whole. (a) Preprocessing of data by splitting into tonic and phasic components, (b) Screening of thresholds with chosen threshold marked with bolded rectangle, (c) Pulses extracted at chosen threshold, (d) Full KS-plot showing goodness-of-fit at chosen threshold

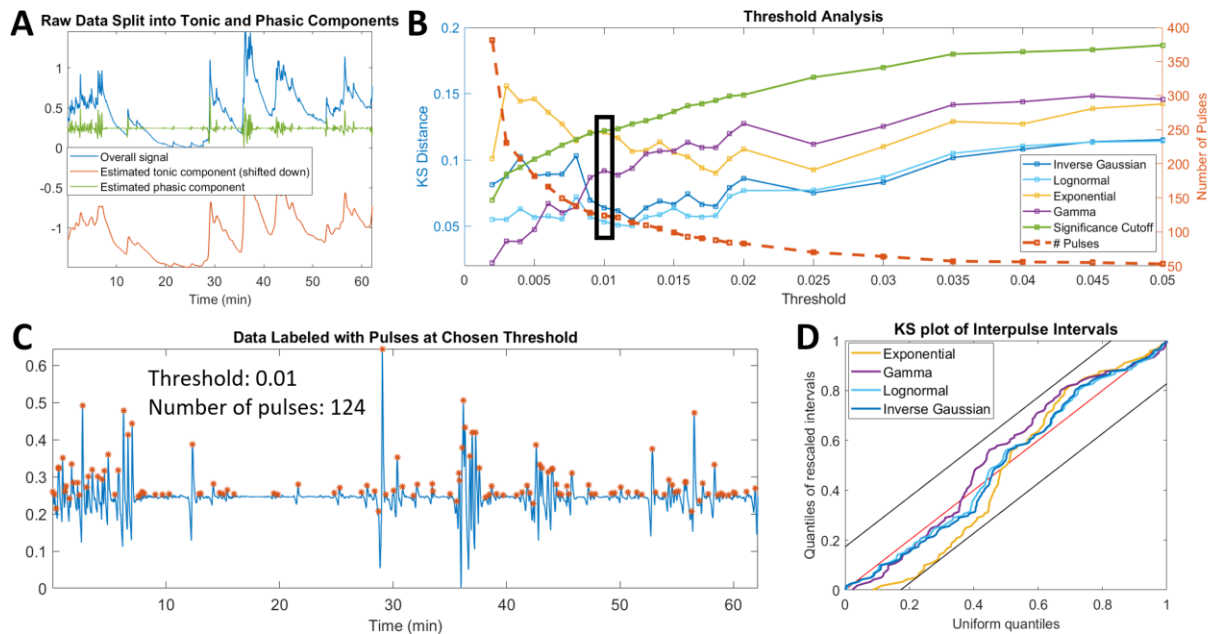


Fig. S5. Results for Subject S7 from the awake and at rest cohort, showing agreement with the trends of the cohort as a whole. (a) Preprocessing of data by splitting into tonic and phasic components, (b) Screening of thresholds with chosen threshold marked with bolded rectangle, (c) Pulses extracted at chosen threshold, (d) Full KS-plot showing goodness-of-fit at chosen threshold



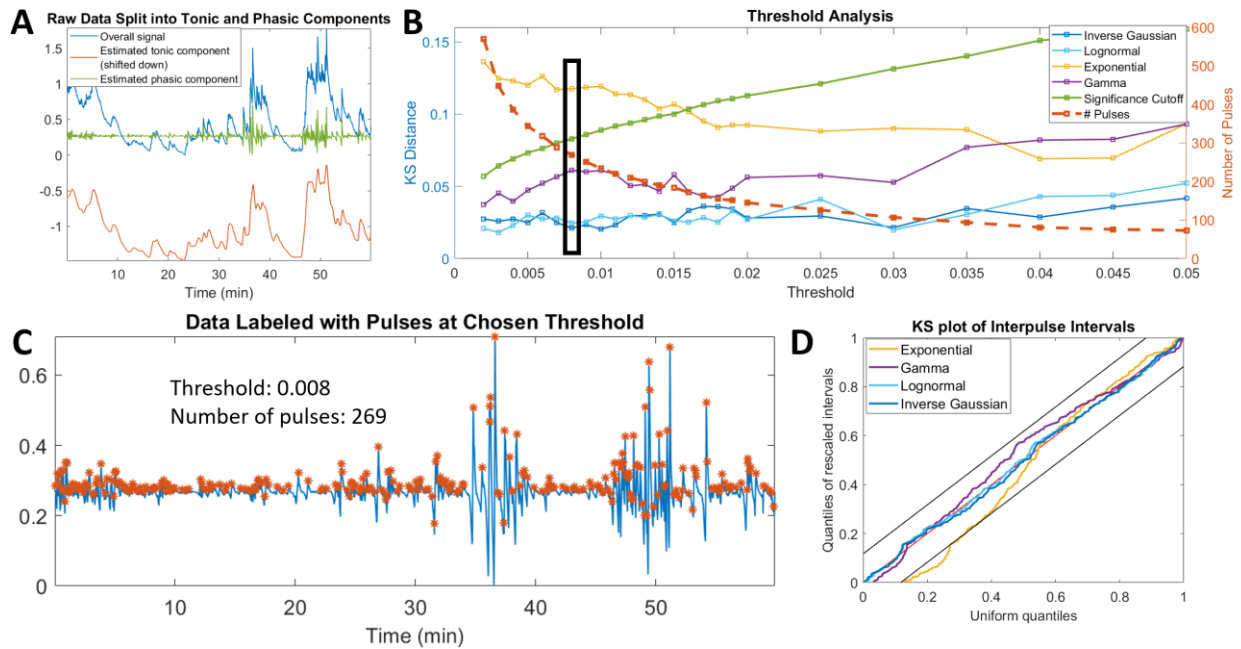


Fig. S6. Results for Subject S8 from the awake and at rest cohort, showing agreement with the trends of the cohort as a whole. (a) Preprocessing of data by splitting into tonic and phasic components, (b) Screening of thresholds with chosen threshold marked with bolded rectangle, (c) Pulses extracted at chosen threshold, (d) Full KS-plot showing goodness-of-fit at chosen threshold

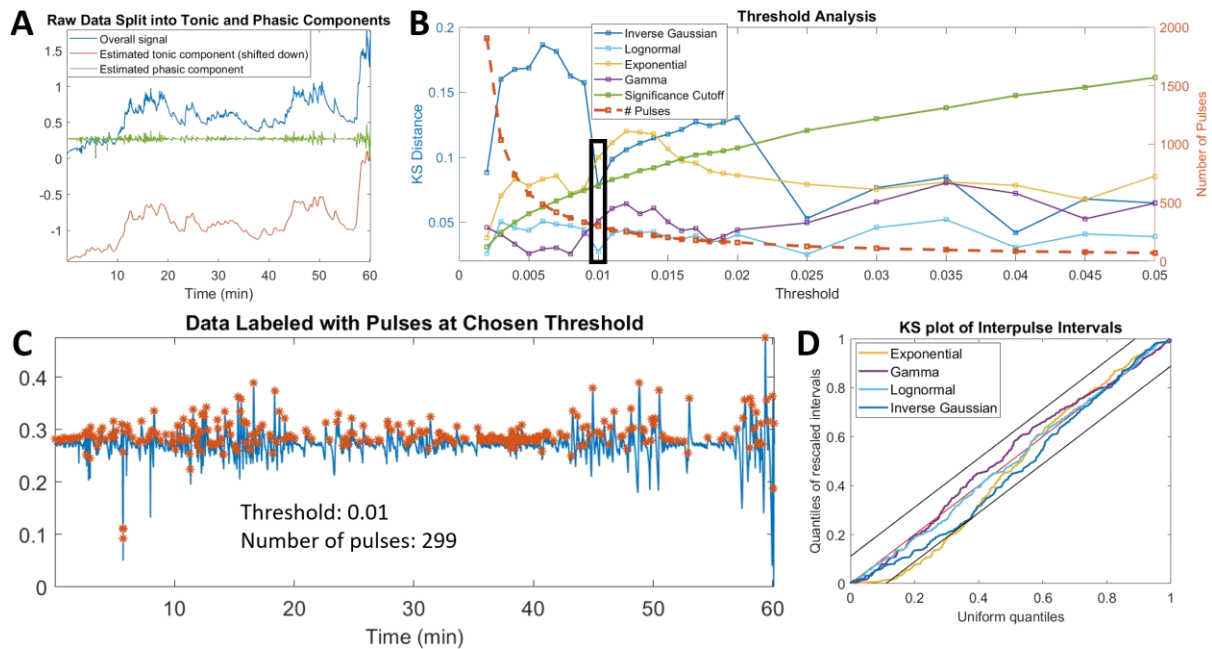


Fig. S7. Results for Subject S9 from the awake and at rest cohort, showing agreement with the trends of the cohort as a whole. (a) Preprocessing of data by splitting into tonic and phasic components, (b) Screening of thresholds with chosen threshold marked with bolded rectangle, (c) Pulses extracted at chosen threshold, (d) Full KS-plot showing goodness-of-fit at chosen threshold

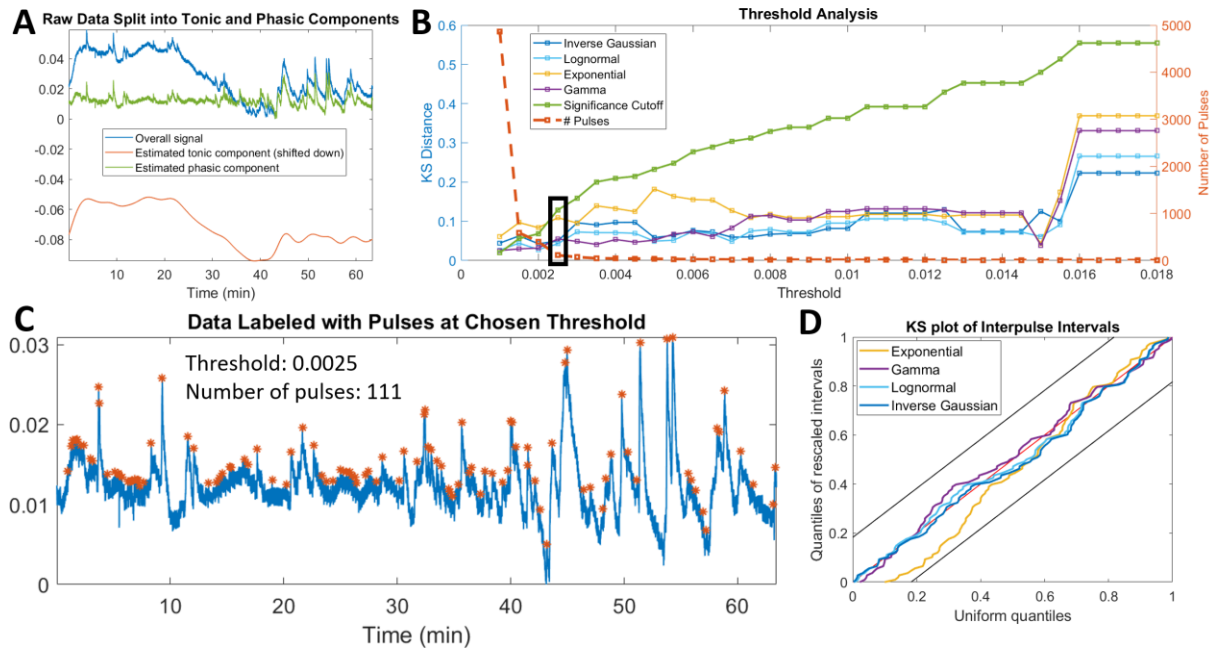


Fig. S8. Results for Subject S10 from the awake and at rest cohort, showing agreement with the trends of the cohort as a whole. (a) Preprocessing of data by splitting into tonic and phasic components, (b) Screening of thresholds with chosen threshold marked with bolded rectangle, (c) Pulses extracted at chosen threshold, (d) Full KS-plot showing goodness-of-fit at chosen threshold

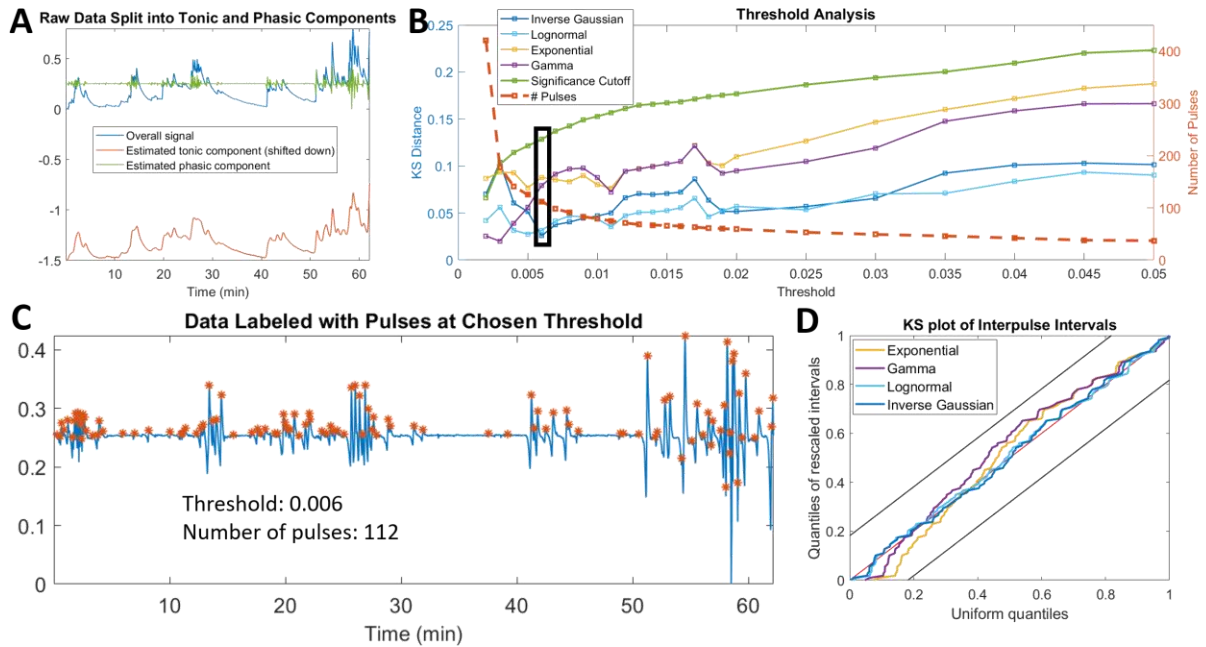


Fig. S9. Results for Subject S11 from the awake and at rest cohort, showing agreement with the trends of the cohort as a whole. (a) Preprocessing of data by splitting into tonic and phasic components, (b) Screening of thresholds with chosen threshold marked with bolded rectangle, (c) Pulses extracted at chosen threshold, (d) Full KS-plot showing goodness-of-fit at chosen threshold

# PROPOFOL SEDATION COHORT

TABLE S-III  
AIC RESULTS FOR THE PROPOFOL SEDATION COHORT

	Thresh	Num. pulses	IG	LogN	Gamma	Exp
P1	0.035	727	4892.359	<b>4862.670</b>	5077.407	5159.771
P2	0.020	383	<b>3232.026</b>	3243.971	3370.773	3370.680
P3	0.035	762	5259.942	<b>5259.534</b>	5470.766	5468.826
P4	0.025	1010	7169.775	<b>7130.224</b>	7440.207	7440.261
P5	0.055	566	4293.377	<b>4260.999</b>	4400.896	4428.529
P6	0.020	838	5512.970	<b>5490.560</b>	5701.877	5772.100
P7	0.035	1250	<b>7489.674</b>	7498.297	7771.781	7866.955
P8	0.040	494	<b>3837.628</b>	3847.869	3991.711	3990.792
P9	0.055	575	4479.243	<b>4448.334</b>	4522.479	4570.867
P10	0.021	627	<b>4617.829</b>	4651.130	4874.572	4917.459
P11	0.030	778	5355.024	<b>5332.838</b>	5392.146	5523.467

The best model for each subject is indicated in bold.

Thresh = threshold, IG = inverse Gaussian, LogN = lognormal, Exp = exponential

TABLE S-IV  
SETTLING RATE RESULTS FOR THE PROPOFOL SEDATION COHORT

	IG	LogN	Gamma	Exp
P1	0.047	0	0.125	0.078
P2	0.008	0	0.030	0.033
P3	0.021	0	0.076	0.075
P4	0.020	0	0.072	0.068
P5	0.023	0	0.073	0.054
P6	0.045	0	0.129	0.087
P7	0.058	0	0.170	0.117
P8	0.012	0	0.045	0.048
P9	0.023	0	0.076	0.051
P10	0.009	0	0.039	0.054
P11	0.045	0	0.140	0.078

IG = inverse Gaussian, LogN = lognormal, Exp = exponential

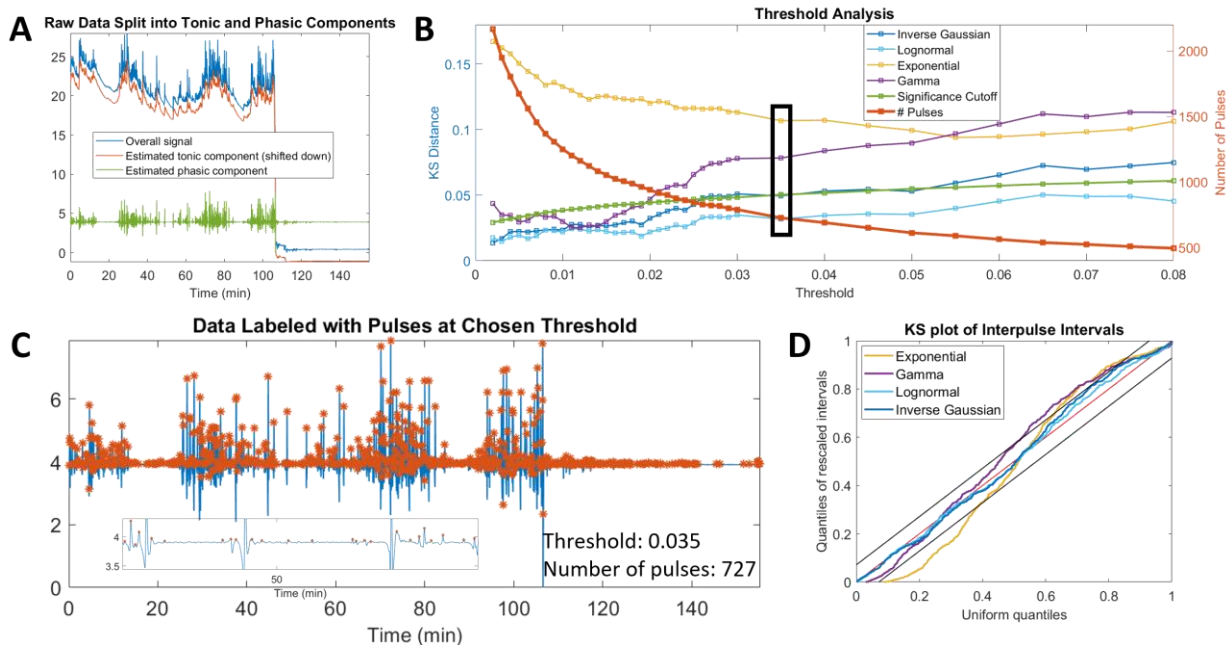


Fig. S10. Results for Subject P1 from the propofol sedation cohort, showing agreement with the trends of the cohort as a whole. (a) Preprocessing of data by splitting into tonic and phasic components, (b) Screening of thresholds with chosen threshold marked with bolded rectangle, (c) Pulses extracted at chosen threshold, (d) Full KS-plot showing goodness-of-fit at chosen threshold

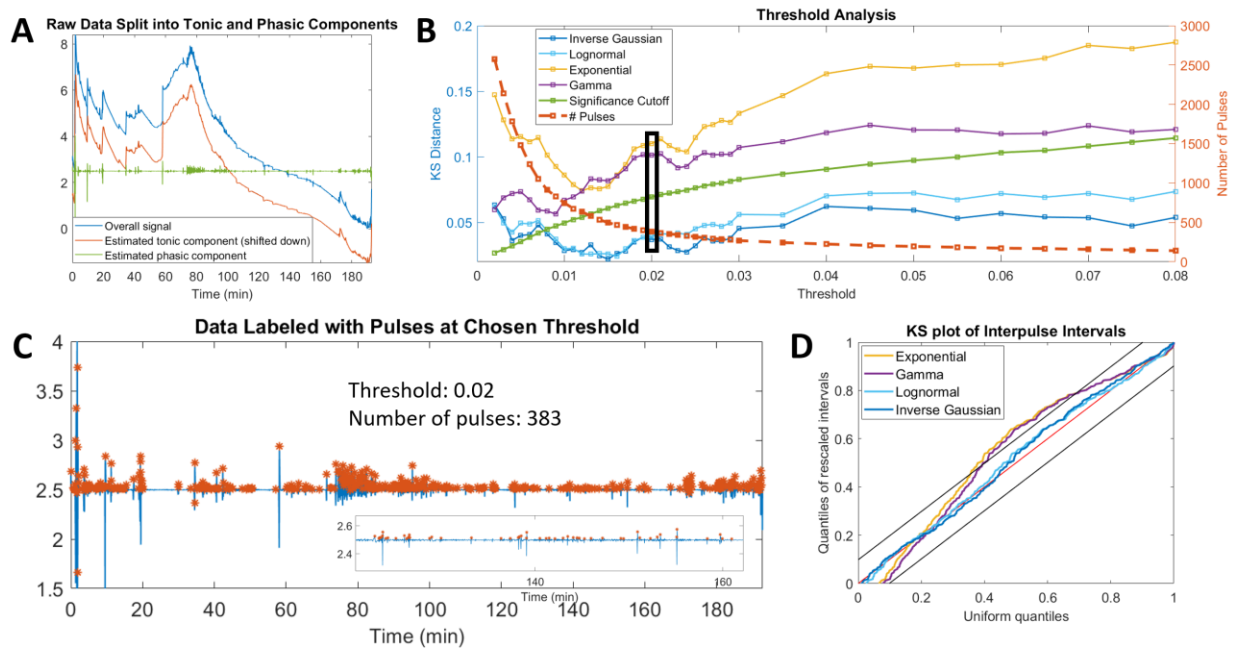


Fig. S11. Results for Subject P2 from the propofol sedation cohort, showing agreement with the trends of the cohort as a whole. (a) Preprocessing of data by splitting into tonic and phasic components, (b) Screening of thresholds with chosen threshold marked with bolded rectangle, (c) Pulses extracted at chosen threshold, (d) Full KS-plot showing goodness-of-fit at chosen threshold

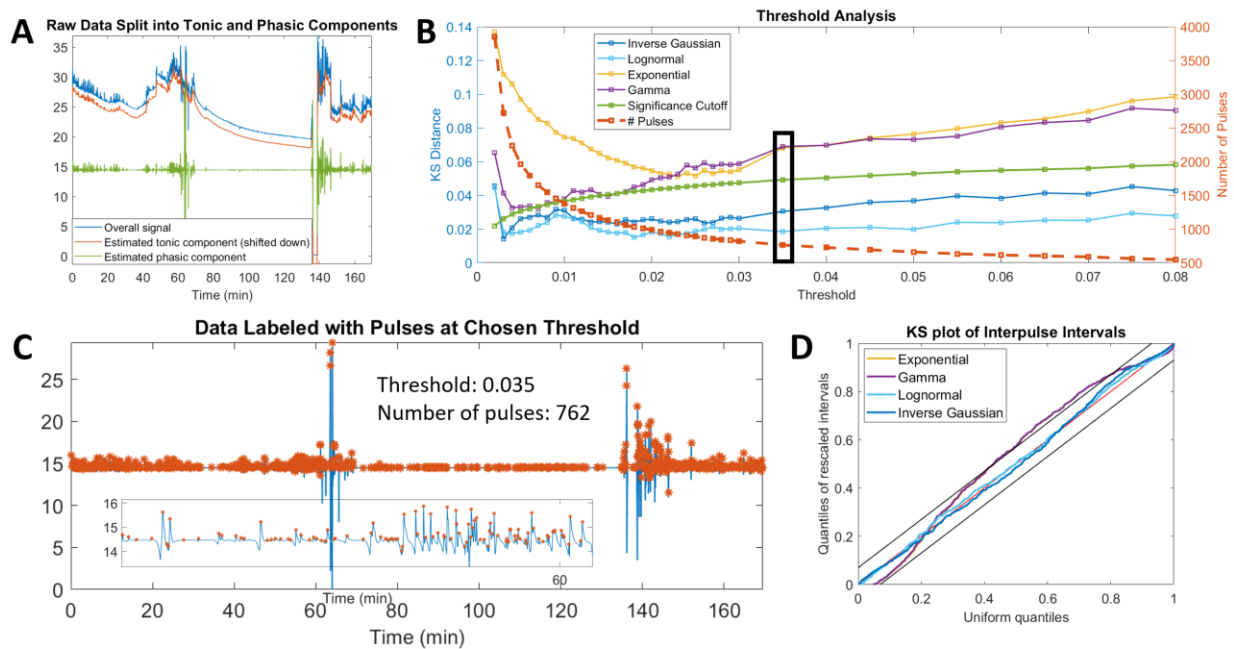


Fig. S12. Results for Subject P3 from the propofol sedation cohort, showing agreement with the trends of the cohort as a whole. (a) Preprocessing of data by splitting into tonic and phasic components, (b) Screening of thresholds with chosen threshold marked with bolded rectangle, (c) Pulses extracted at chosen threshold, (d) Full KS-plot showing goodness-of-fit at chosen threshold

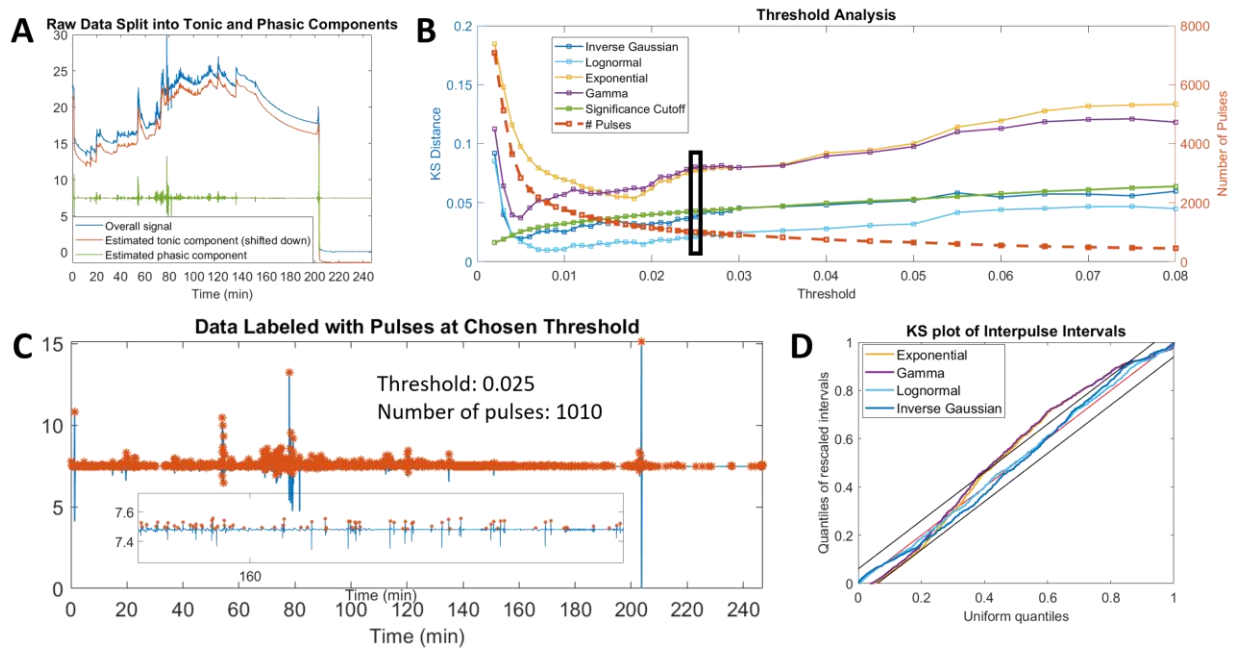


Fig. S13. Results for Subject P4 from the propofol sedation cohort, showing agreement with the trends of the cohort as a whole. (a) Preprocessing of data by splitting into tonic and phasic components, (b) Screening of thresholds with chosen threshold marked with bolded rectangle, (c) Pulses extracted at chosen threshold, (d) Full KS-plot showing goodness-of-fit at chosen threshold

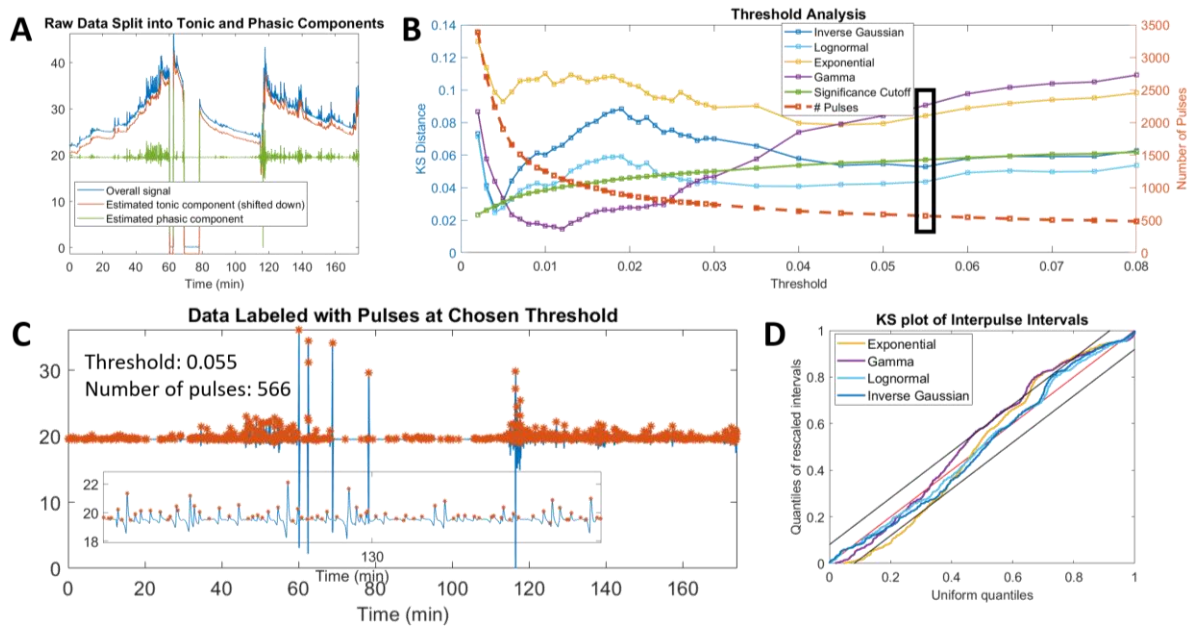


Fig. S14. Results for Subject P5 from the propofol sedation cohort, showing agreement with the trends of the cohort as a whole. (a) Preprocessing of data by splitting into tonic and phasic components, (b) Screening of thresholds with chosen threshold marked with bolded rectangle, (c) Pulses extracted at chosen threshold, (d) Full KS-plot showing goodness-of-fit at chosen threshold



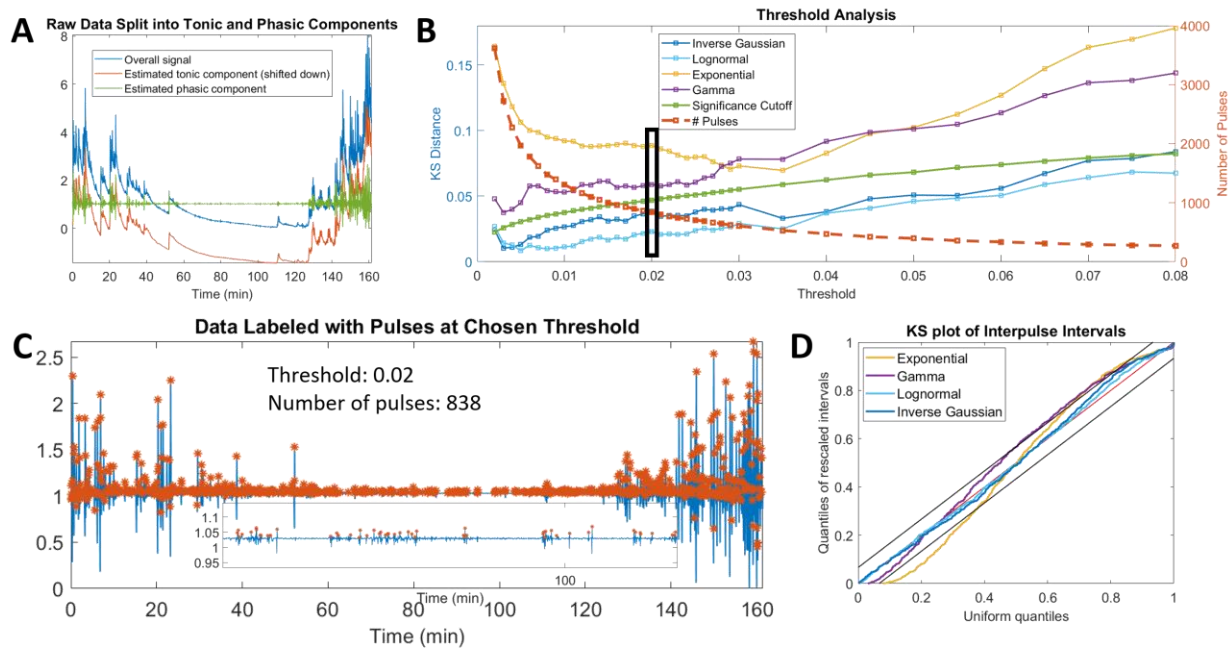


Fig. S15. Results for Subject P6 from the propofol sedation cohort, showing agreement with the trends of the cohort as a whole. (a) Preprocessing of data by splitting into tonic and phasic components, (b) Screening of thresholds with chosen threshold marked with bolded rectangle, (c) Pulses extracted at chosen threshold, (d) Full KS-plot showing goodness-of-fit at chosen threshold

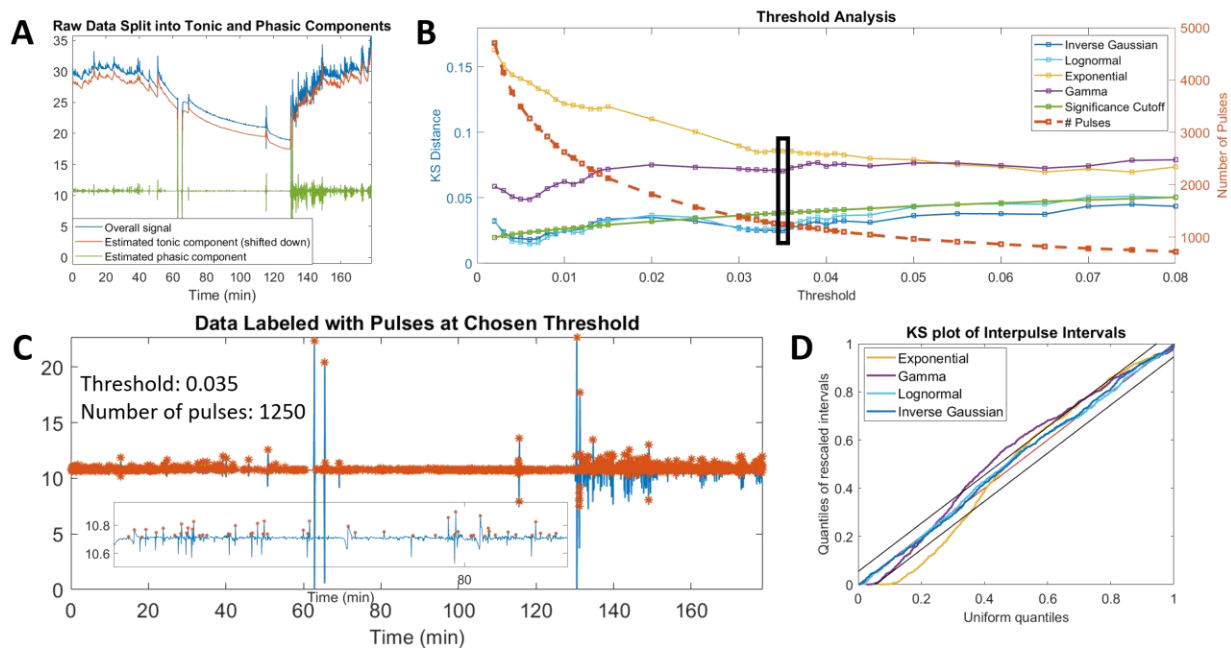


Fig. S16. Results for Subject P7 from the propofol sedation cohort, showing agreement with the trends of the cohort as a whole. (a) Preprocessing of data by splitting into tonic and phasic components, (b) Screening of thresholds with chosen threshold marked with bolded rectangle, (c) Pulses extracted at chosen threshold, (d) Full KS-plot showing goodness-of-fit at chosen threshold

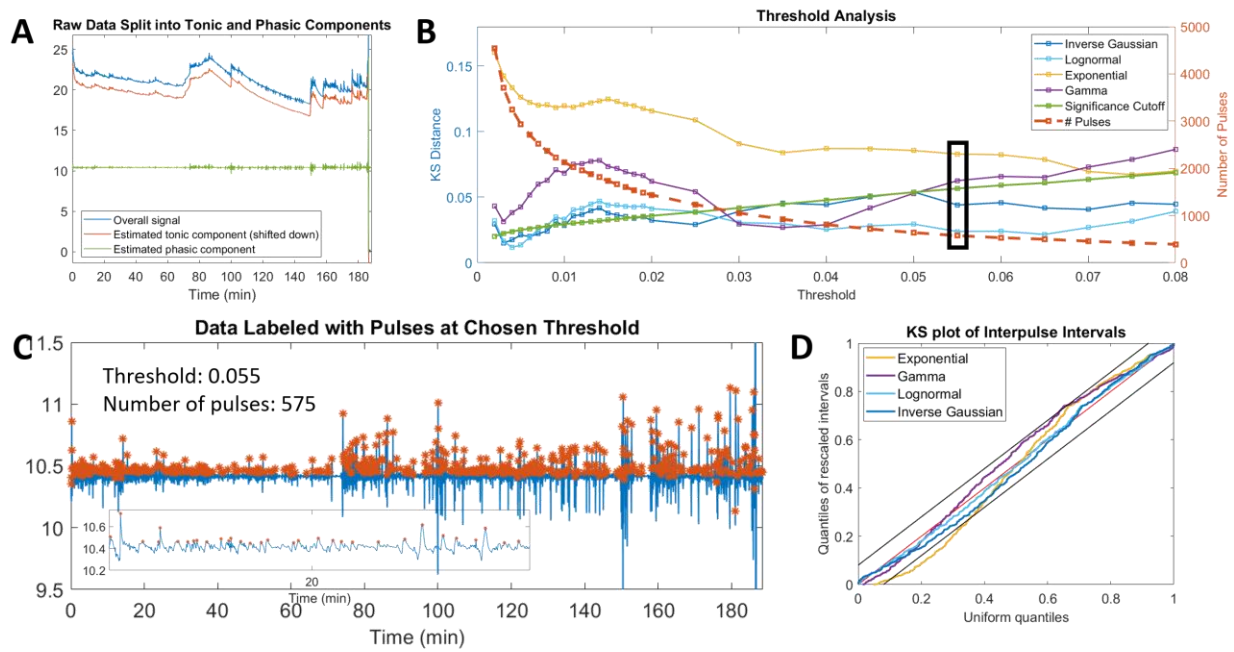


Fig. S17. Results for Subject P9 from the propofol sedation cohort, showing agreement with the trends of the cohort as a whole. (a) Preprocessing of data by splitting into tonic and phasic components, (b) Screening of thresholds with chosen threshold marked with bolded rectangle, (c) Pulses extracted at chosen threshold, (d) Full KS-plot showing goodness-of-fit at chosen threshold

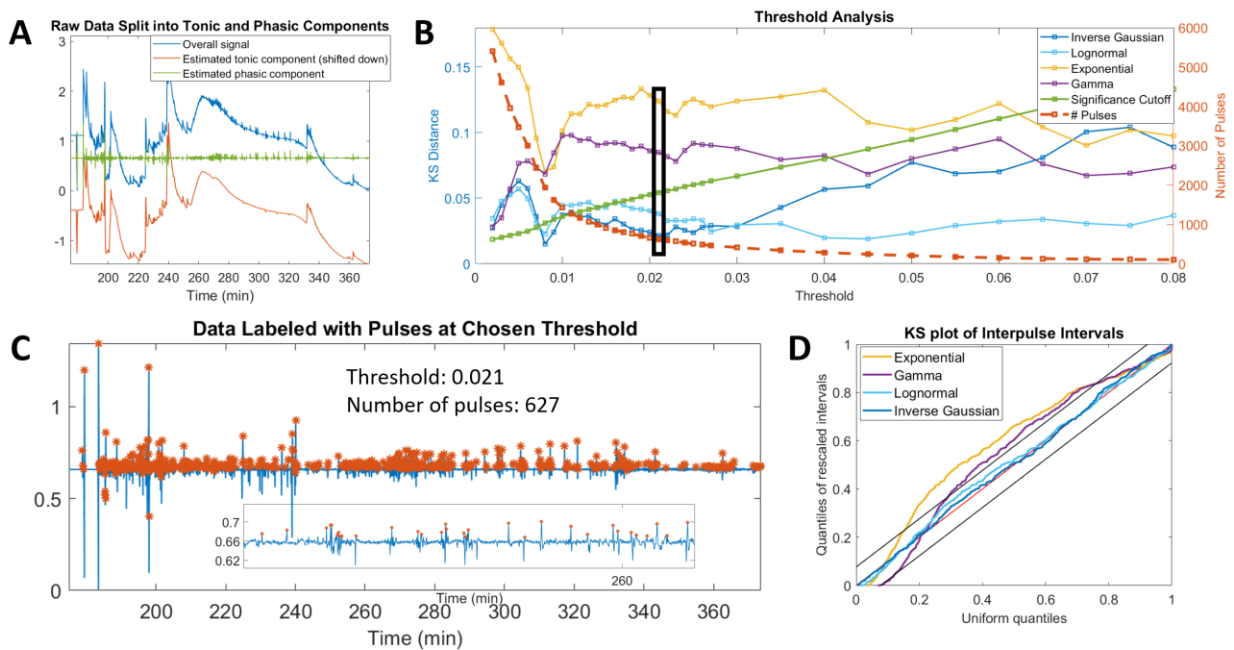


Fig. S18. Results for Subject P10 from the propofol sedation cohort, showing agreement with the trends of the cohort as a whole. (a) Preprocessing of data by splitting into tonic and phasic components, (b) Screening of thresholds with chosen threshold marked with bolded rectangle, (c) Pulses extracted at chosen threshold, (d) Full KS-plot showing goodness-of-fit at chosen threshold

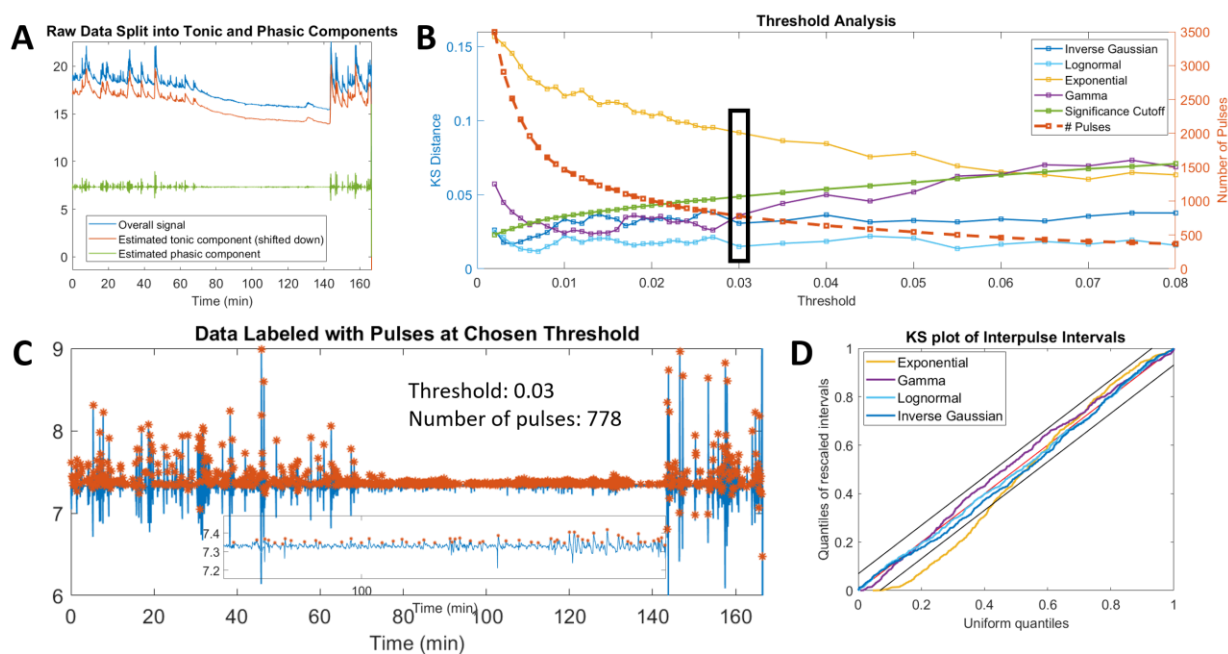


Fig. S19. Results for Subject P11 from the propofol sedation cohort, showing agreement with the trends of the cohort as a whole. (a) Preprocessing of data by splitting into tonic and phasic components, (b) Screening of thresholds with chosen threshold marked with bolded rectangle, (c) Pulses extracted at chosen threshold, (d) Full KS-plot showing goodness-of-fit at chosen threshold

# LEDALAB ALGORITHM RESULTS ON AWAKE AND AT REST COHORT

TABLE S-V  
SUMMARY OF KS-DISTANCE RESULTS FOR THE AWAKE AND AT REST  
COHORT USING THE LEDALAB ALGORITHM

	Num. pulses	Models under Sig. Cutoff
S1	727	IG
S2	383	--
S3	762	--
S4	1010	--
S5	566	--
S6	838	IG, LogN
S7	1250	--
S8	494	--
S9	575	LogN
S10	627	--
S11	778	--

Sig. cutoff = significance cutoff, IG = inverse Gaussian, LogN = lognormal

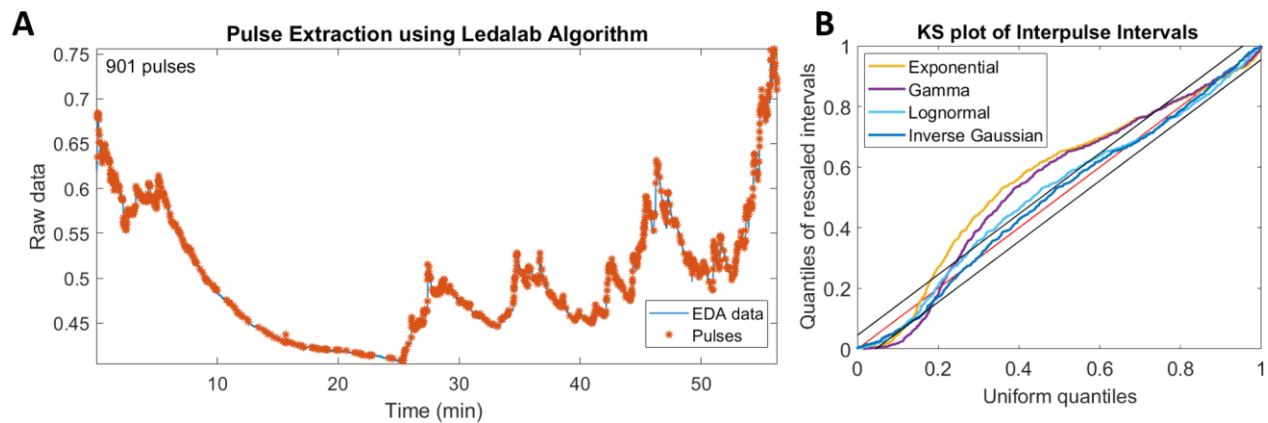


Fig. S20. (a) Pulse selection and (b) goodness-of-fit results using the Ledalab algorithm for Subject S1 from the awake and at rest cohort.

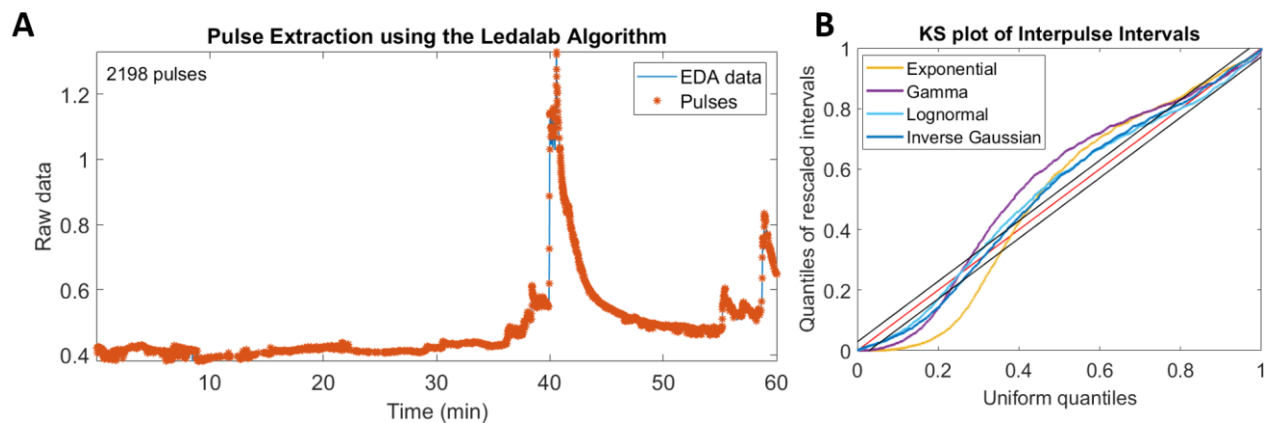


Fig. S21. (a) Pulse selection and (b) goodness-of-fit results using the Ledalab algorithm for Subject S2 from the awake and at rest cohort.

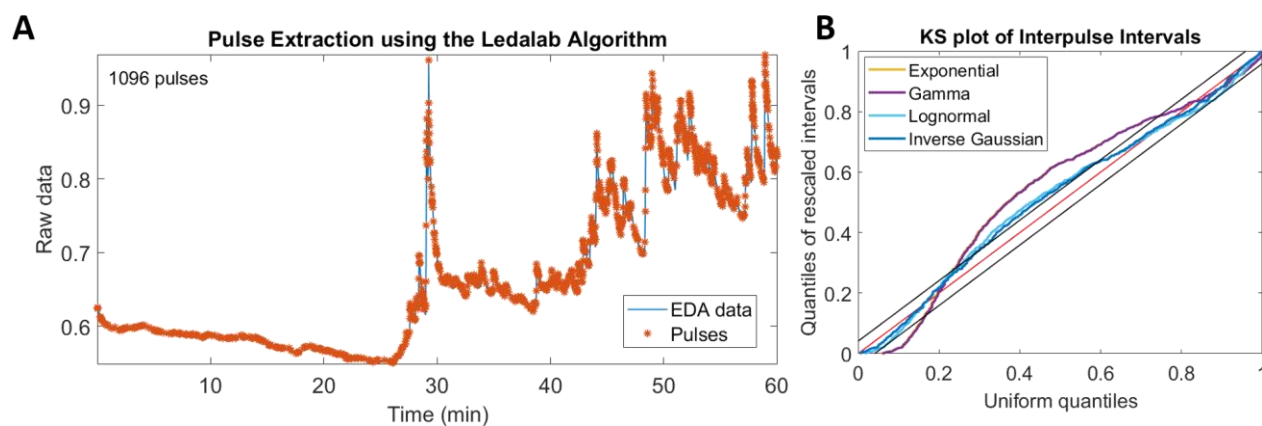


Fig. S22. (a) Pulse selection and (b) goodness-of-fit results using the Ledalab algorithm for Subject S3 from the awake and at rest cohort.

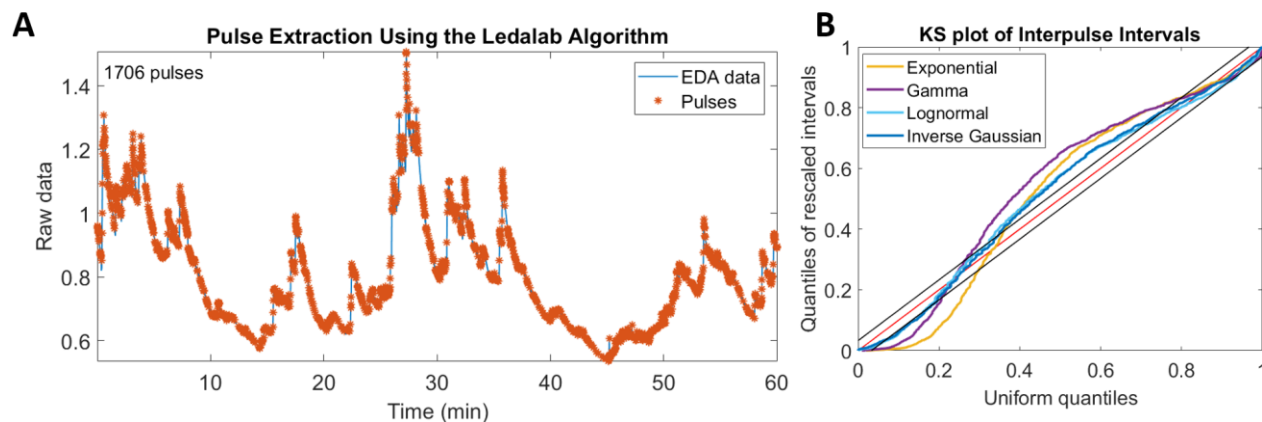


Fig. S23. (a) Pulse selection and (b) goodness-of-fit results using the Ledalab algorithm for Subject S4 from the awake and at rest cohort.

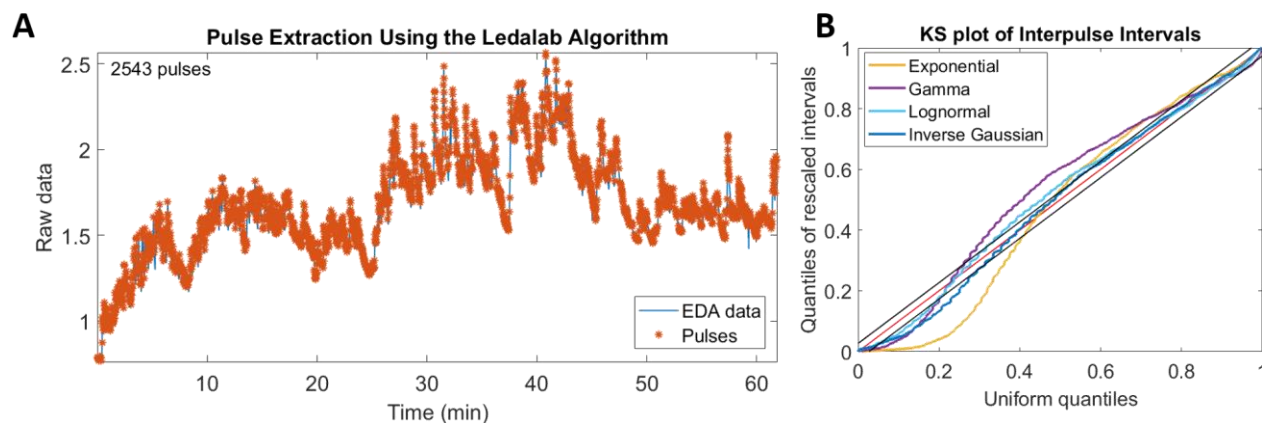


Fig. S24. (a) Pulse selection and (b) goodness-of-fit results using the Ledalab algorithm for Subject S5 from the awake and at rest cohort.



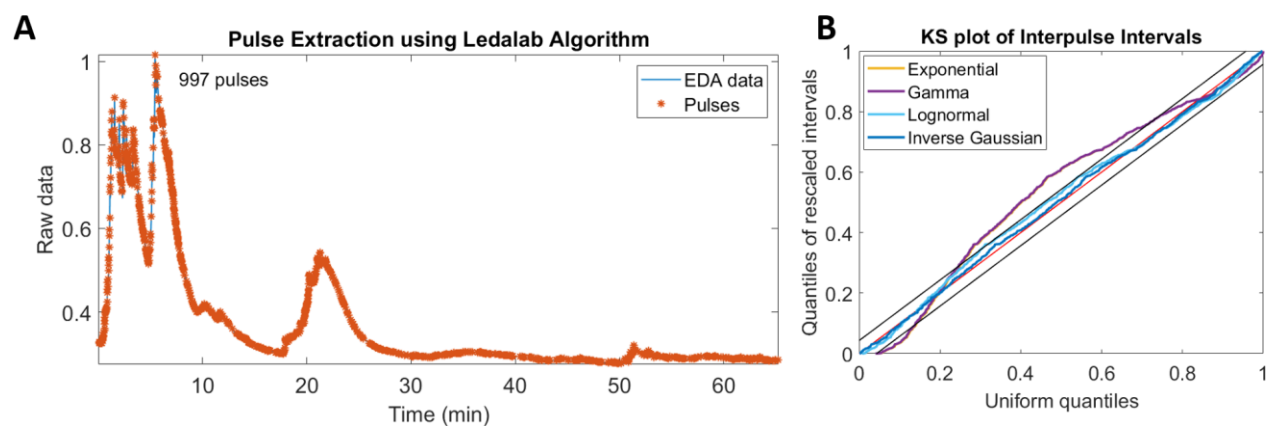


Fig. S25. (a) Pulse selection and (b) goodness-of-fit results using the Ledalab algorithm for Subject S6 from the awake and at rest cohort.

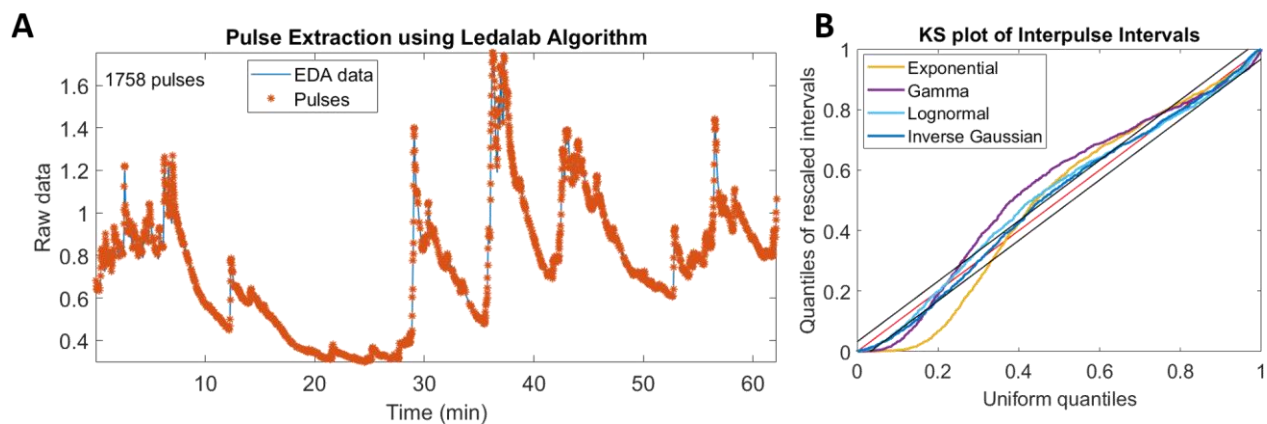


Fig. S26. (a) Pulse selection and (b) goodness-of-fit results using the Ledalab algorithm for Subject S7 from the awake and at rest cohort.

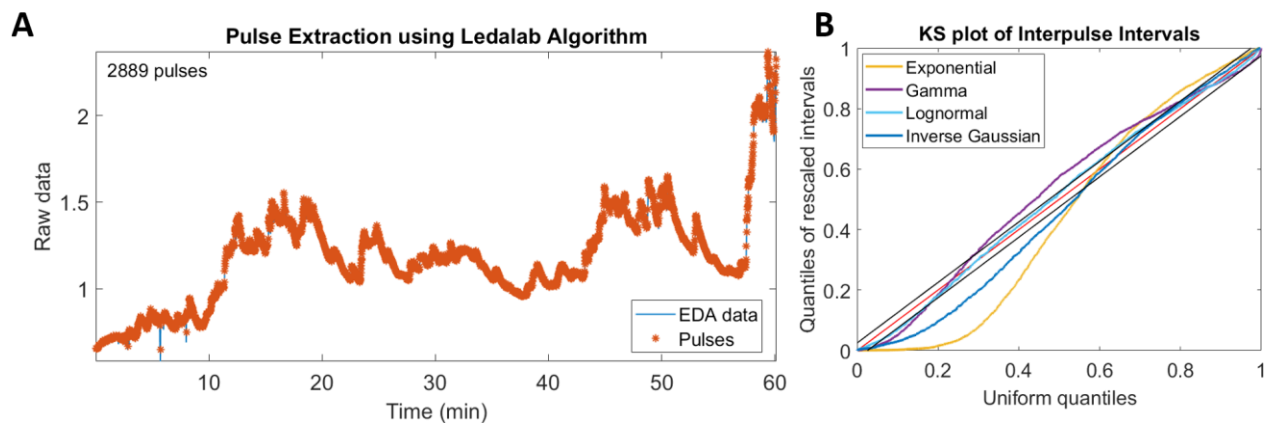


Fig. S27. (a) Pulse selection and (b) goodness-of-fit results using the Ledalab algorithm for Subject S9 from the awake and at rest cohort.

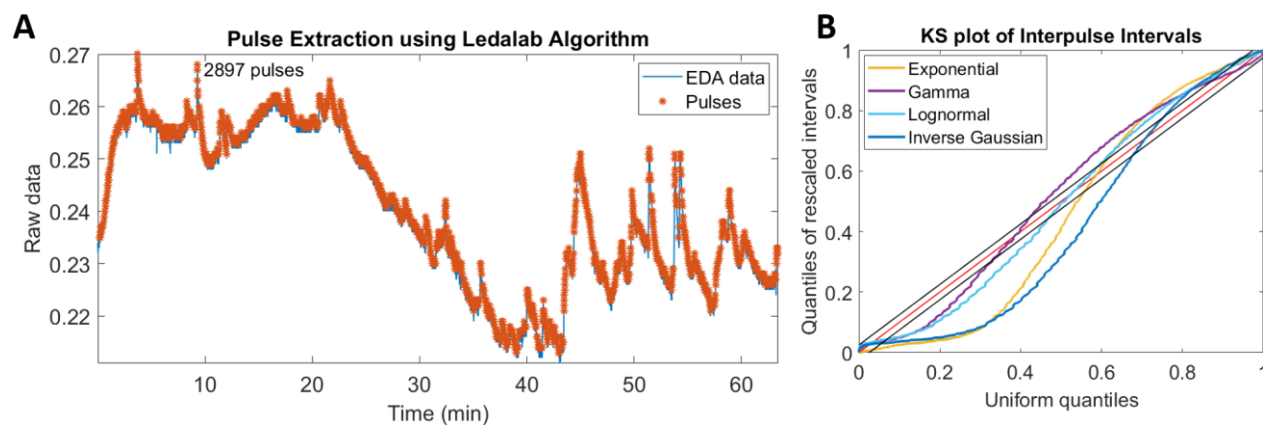


Fig. S29. (a) Pulse selection and (b) goodness-of-fit results using the Ledalab algorithm for Subject S10 from the awake and at rest cohort.

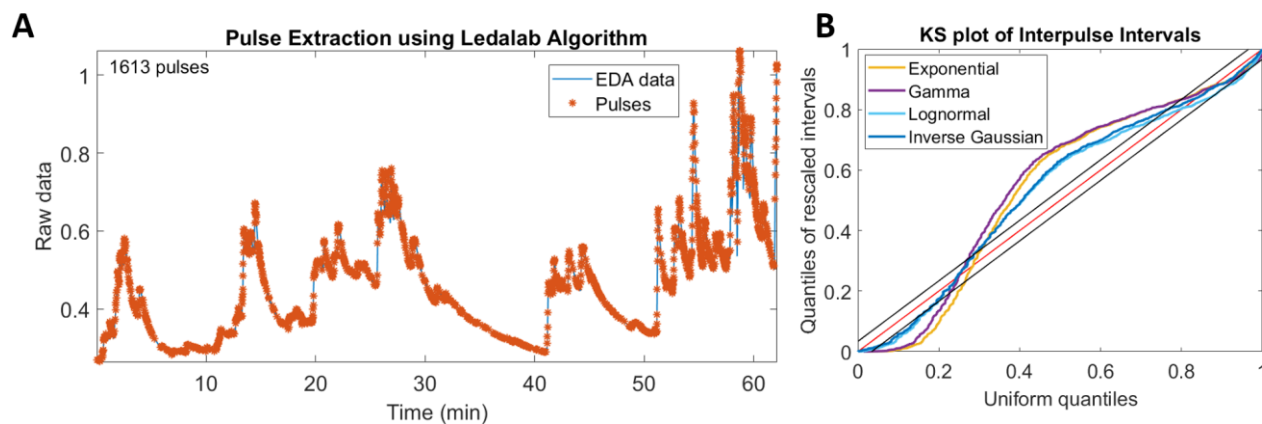


Fig. S28. (a) Pulse selection and (b) goodness-of-fit results using the Ledalab algorithm for Subject S11 from the awake and at rest cohort.

## cvxEDA ALGORITHM RESULTS ON AWAKE AND AT REST COHORT

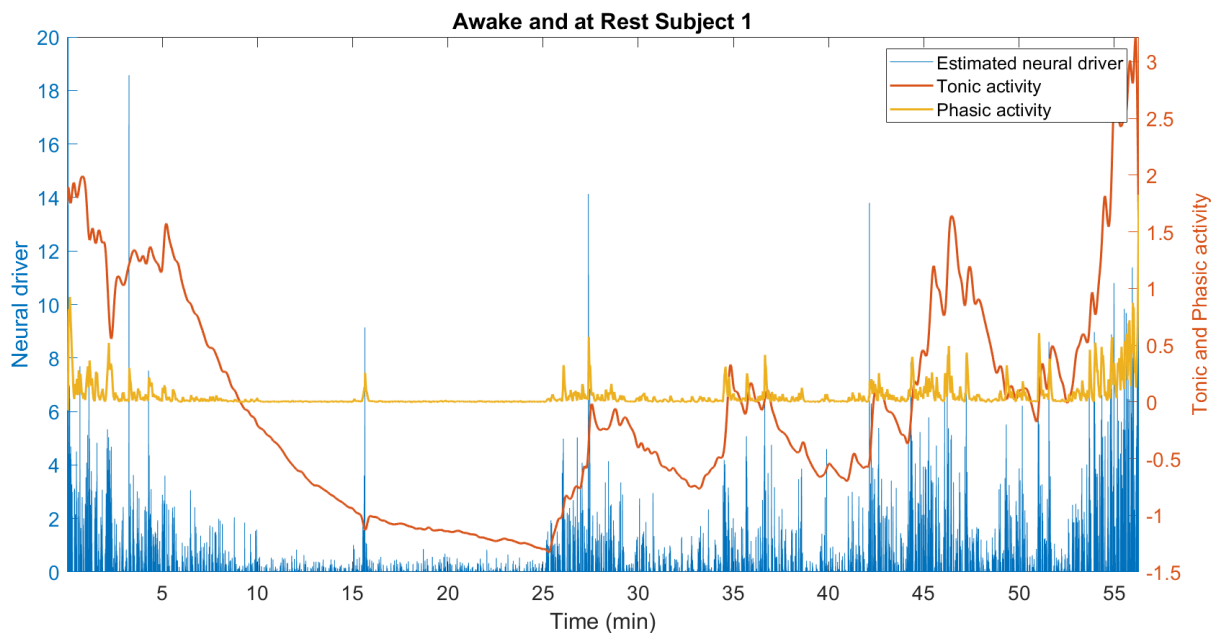


Fig. S30. Results using the cvxEDA algorithm for Subject S1 from the awake and at rest cohort, showing the tonic and phasic components and the estimated neural activity

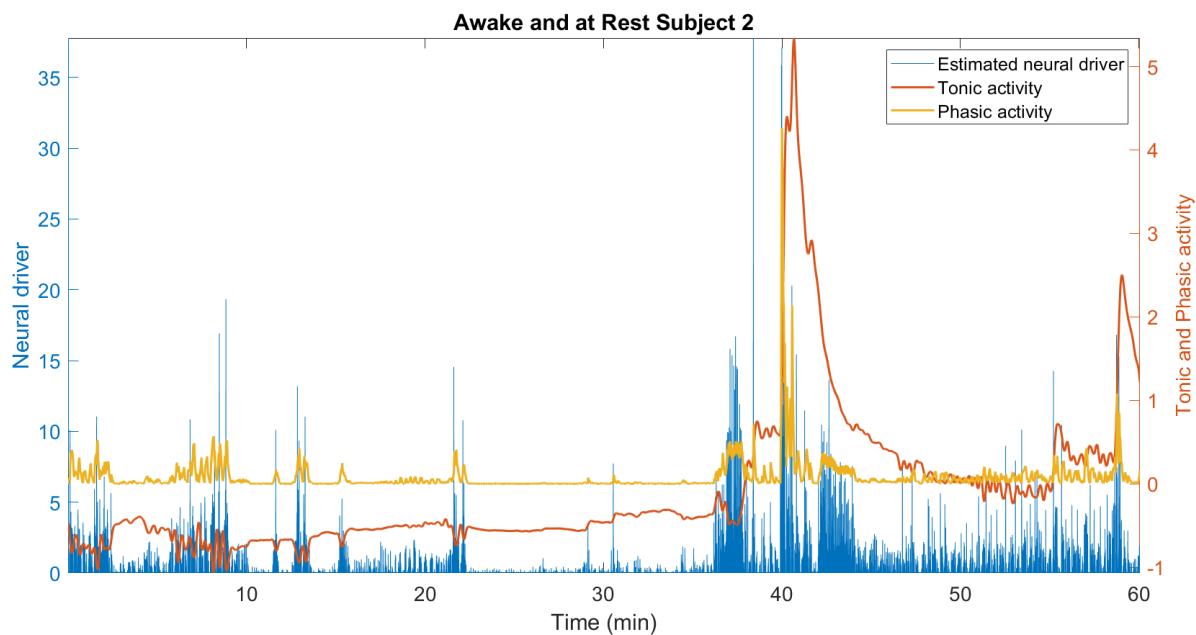


Fig. S31. Results using the cvxEDA algorithm for Subject S2 from the awake and at rest cohort, showing the tonic and phasic components and the estimated neural activity

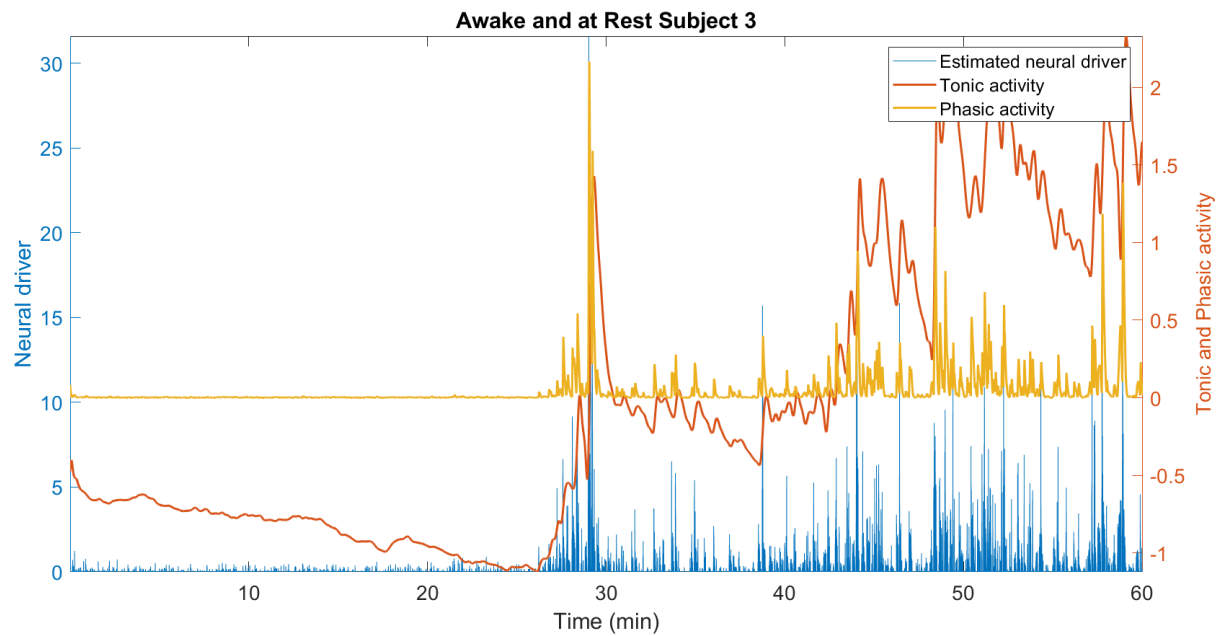


Fig. S32. Results using the cvxEDA algorithm for Subject S3 from the awake and at rest cohort, showing the tonic and phasic components and the estimated neural activity

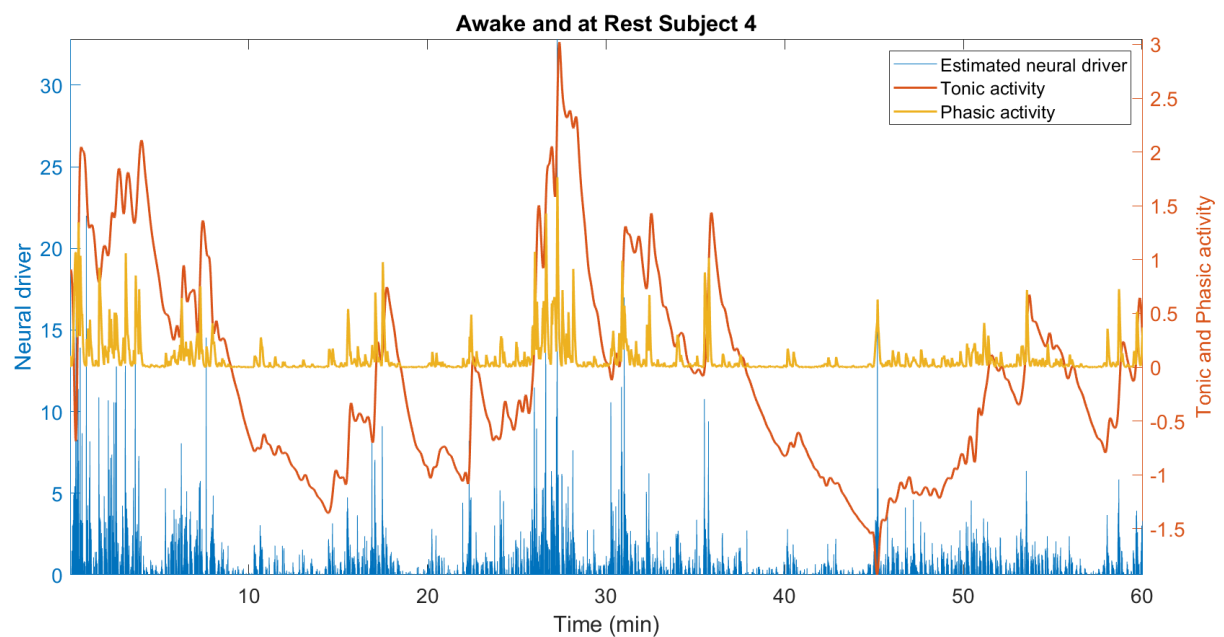


Fig. S33. Results using the cvxEDA algorithm for Subject S4 from the awake and at rest cohort, showing the tonic and phasic components and the estimated neural activity

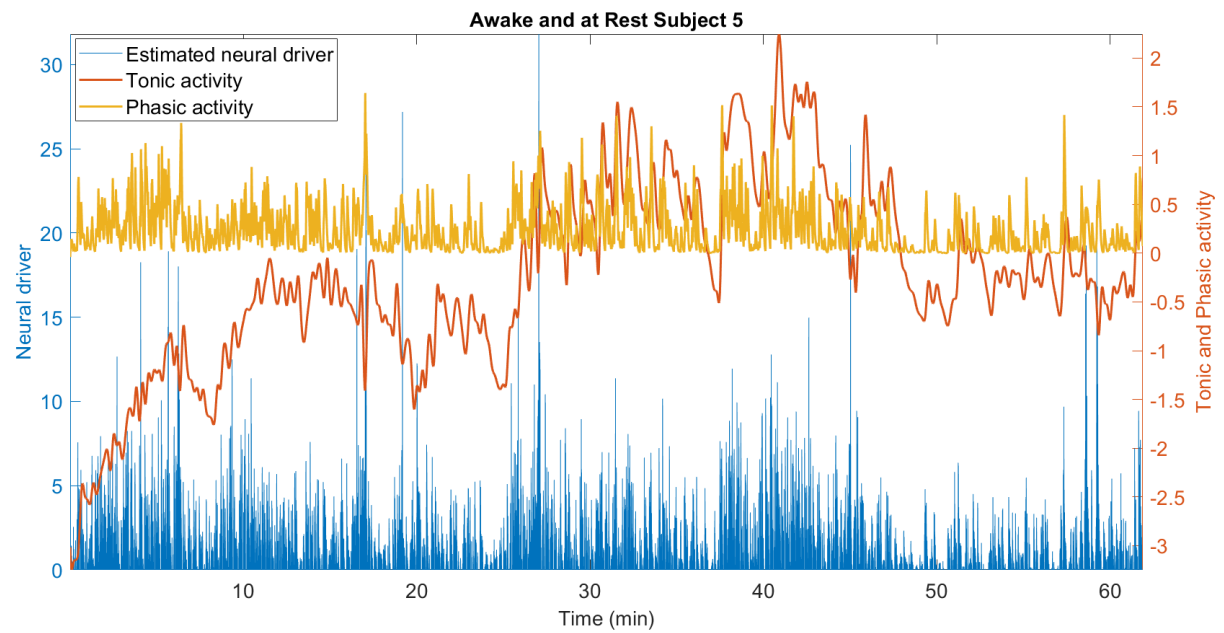


Fig. S34. Results using the cvxEDA algorithm for Subject S5 from the awake and at rest cohort, showing the tonic and phasic components and the estimated neural activity

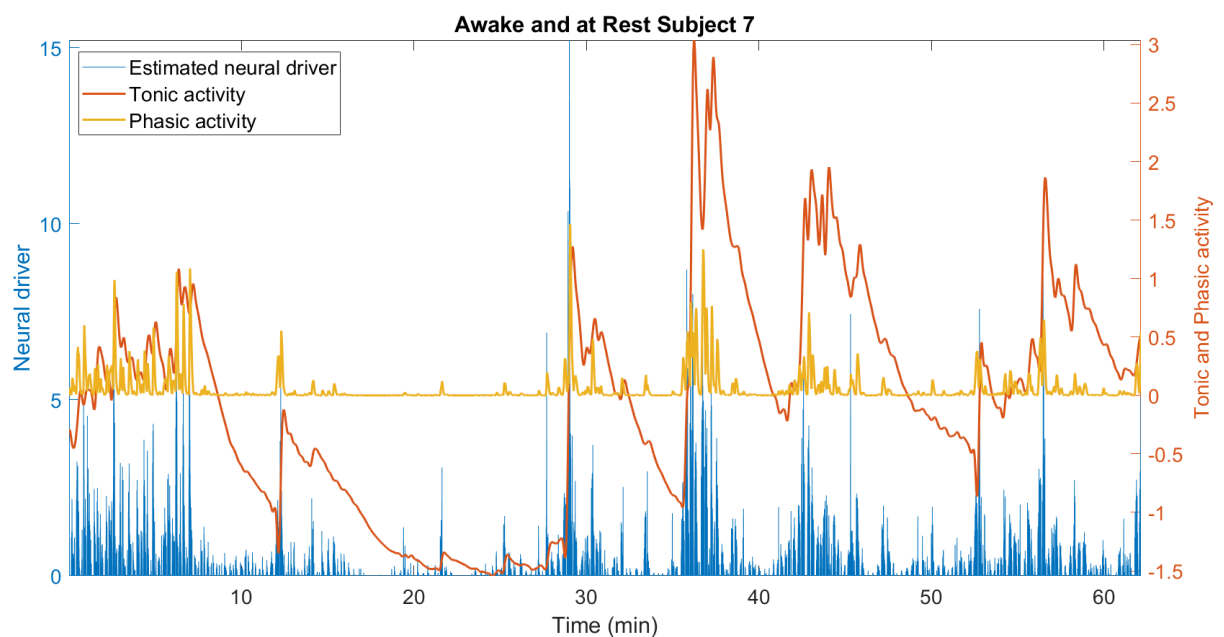


Fig. S35. Results using the cvxEDA algorithm for Subject S7 from the awake and at rest cohort, showing the tonic and phasic components and the estimated neural activity



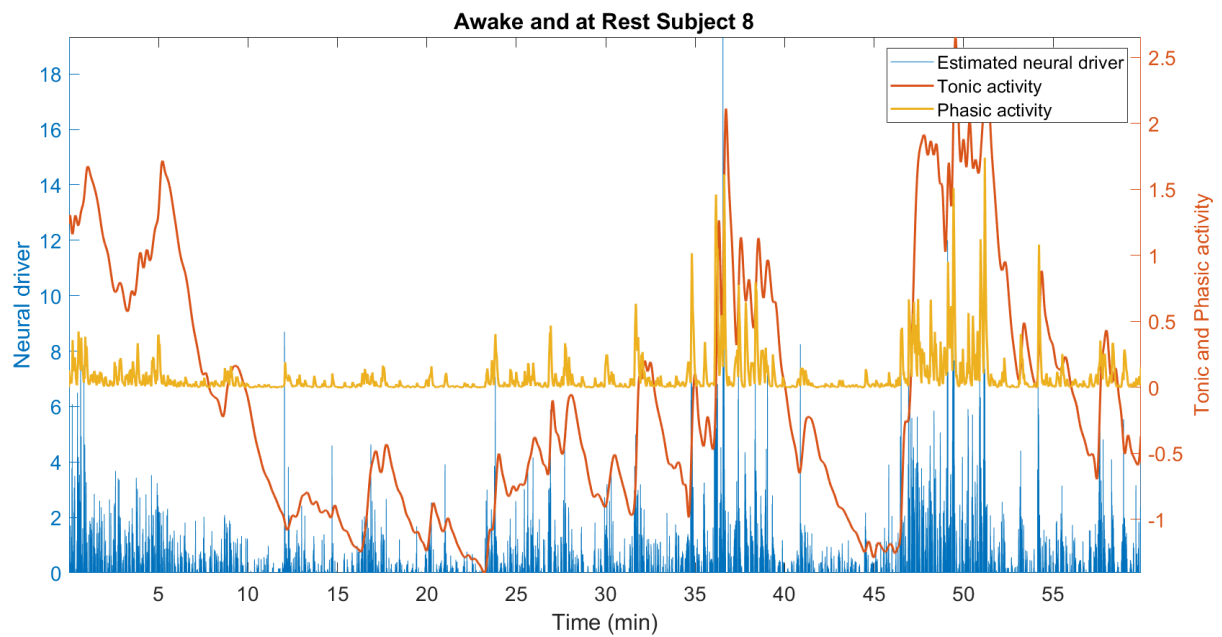


Fig. S36. Results using the cvxEDA algorithm for Subject S8 from the awake and at rest cohort, showing the tonic and phasic components and the estimated neural activity

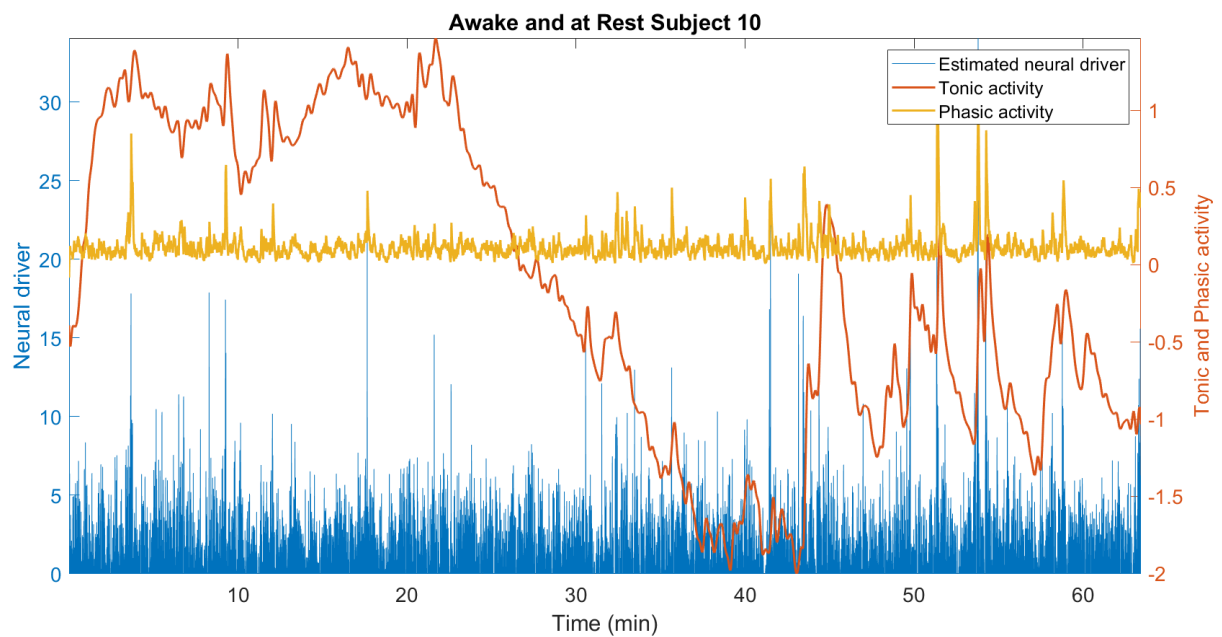


Fig. S37. Results using the cvxEDA algorithm for Subject S10 from the awake and at rest cohort, showing the tonic and phasic components and the estimated neural activity

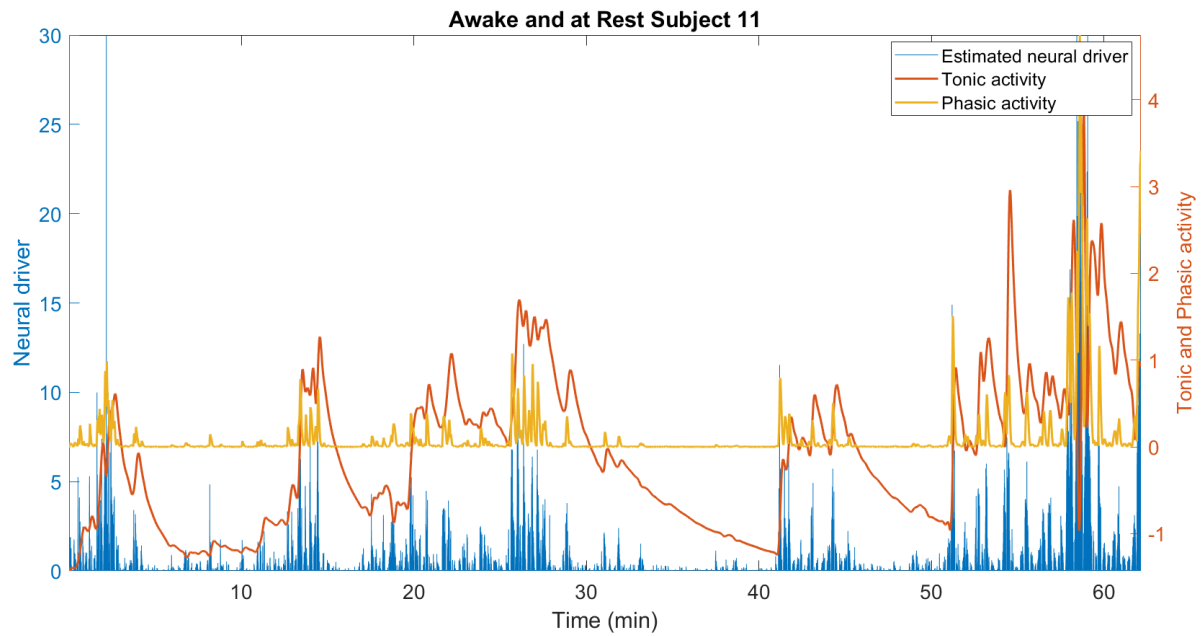


Fig. S38. Results using the cvxEDA algorithm for Subject S11 from the awake and at rest cohort, showing the tonic and phasic components and the estimated neural activity

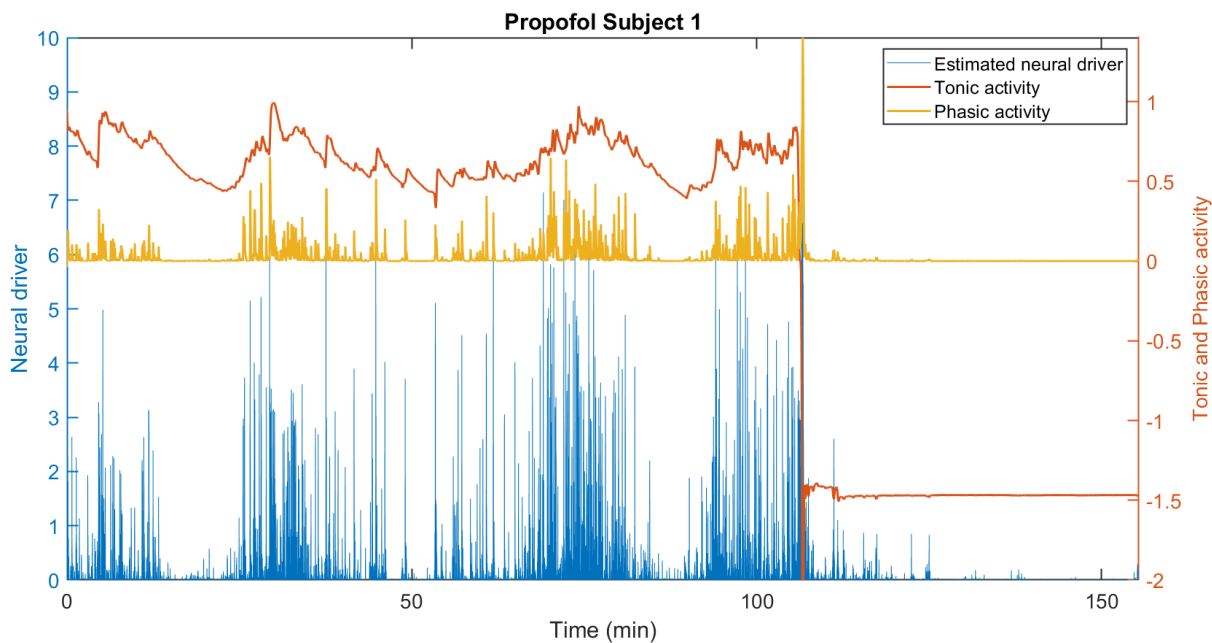
**cvxEDA ALGORITHM RESULTS ON PROPOFOL SEDATION COHORT**

Fig. S39. Results using the cvxEDA algorithm for Subject P1 from the propofol sedation cohort, showing the tonic and phasic components and the estimated neural activity

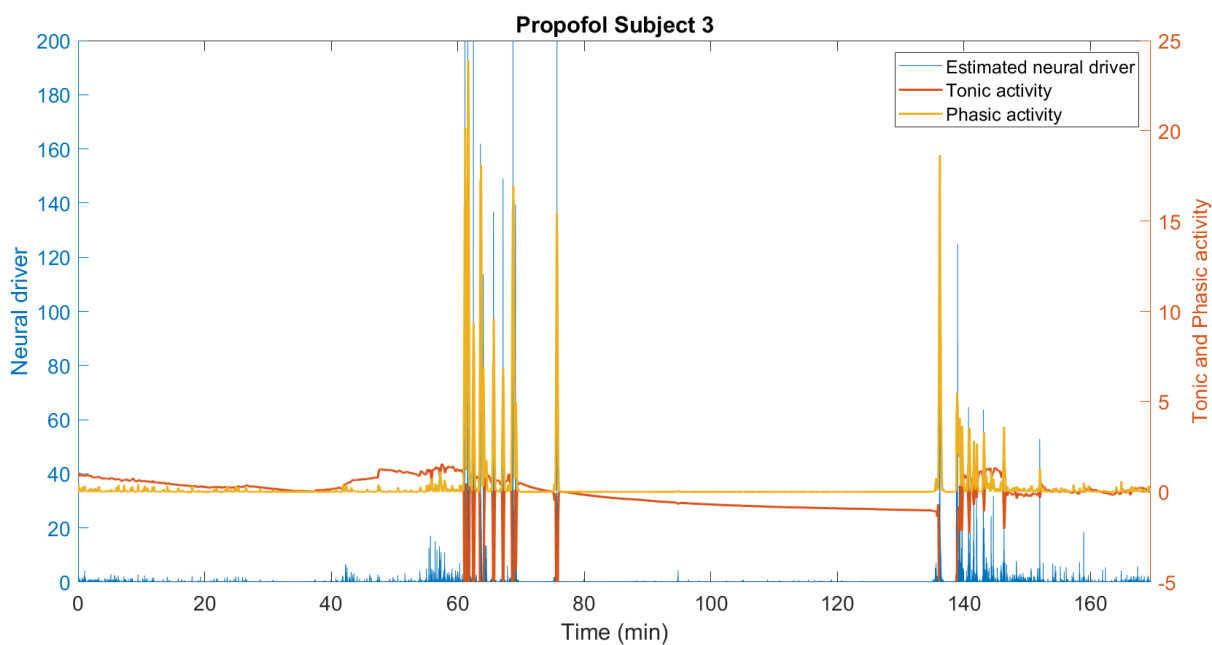


Fig. S40. Results using the cvxEDA algorithm for Subject P3 from the propofol sedation cohort, showing the tonic and phasic components and the estimated neural activity

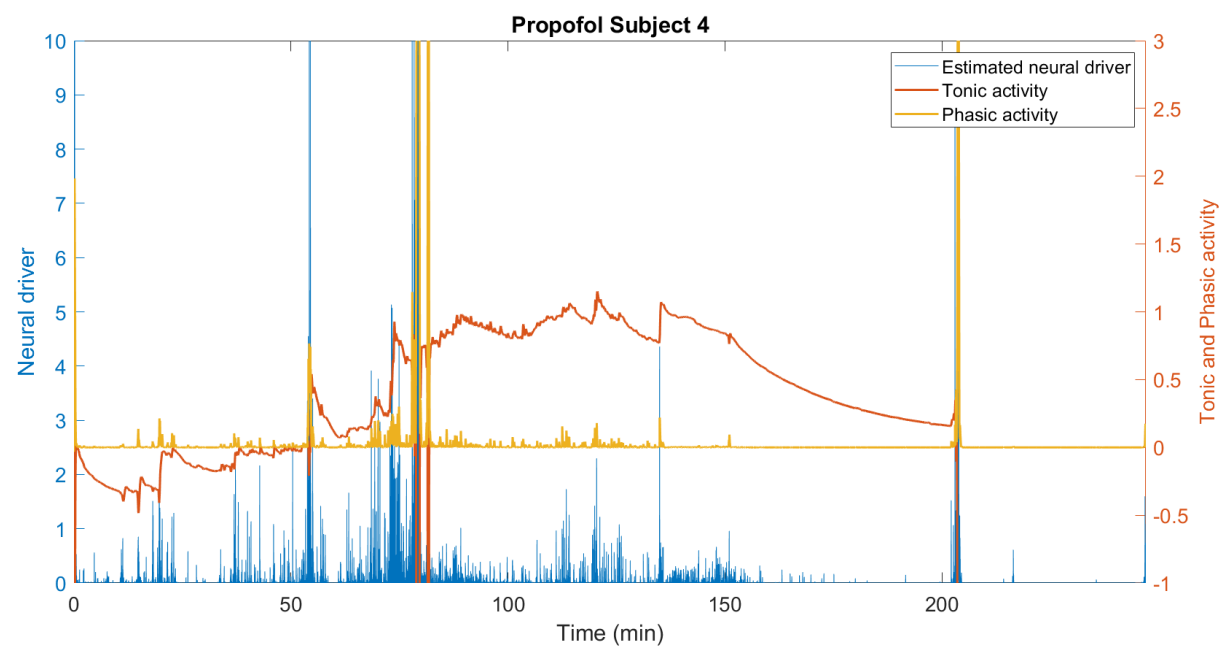


Fig. S41. Results using the cvxEDA algorithm for Subject P4 from the propofol sedation cohort, showing the tonic and phasic components and the estimated neural activity

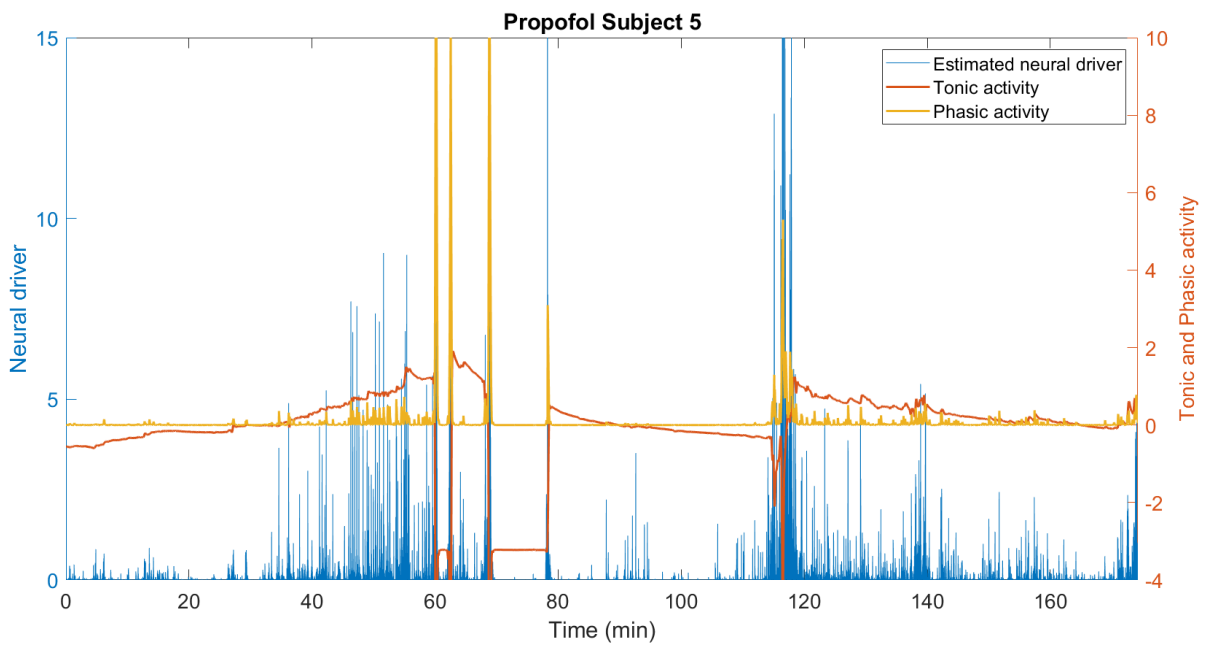


Fig. S42. Results using the cvxEDA algorithm for Subject P5 from the propofol sedation cohort, showing the tonic and phasic components and the estimated neural activity

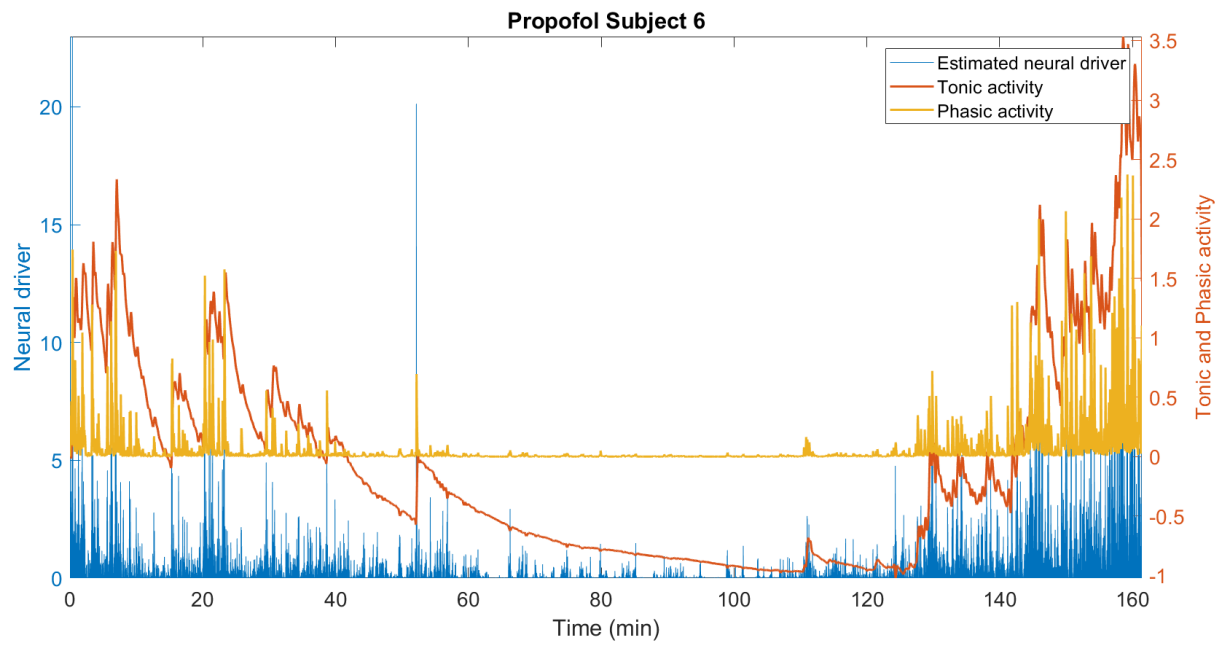


Fig. S43. Results using the cvxEDA algorithm for Subject P6 from the propofol sedation cohort, showing the tonic and phasic components and the estimated neural activity

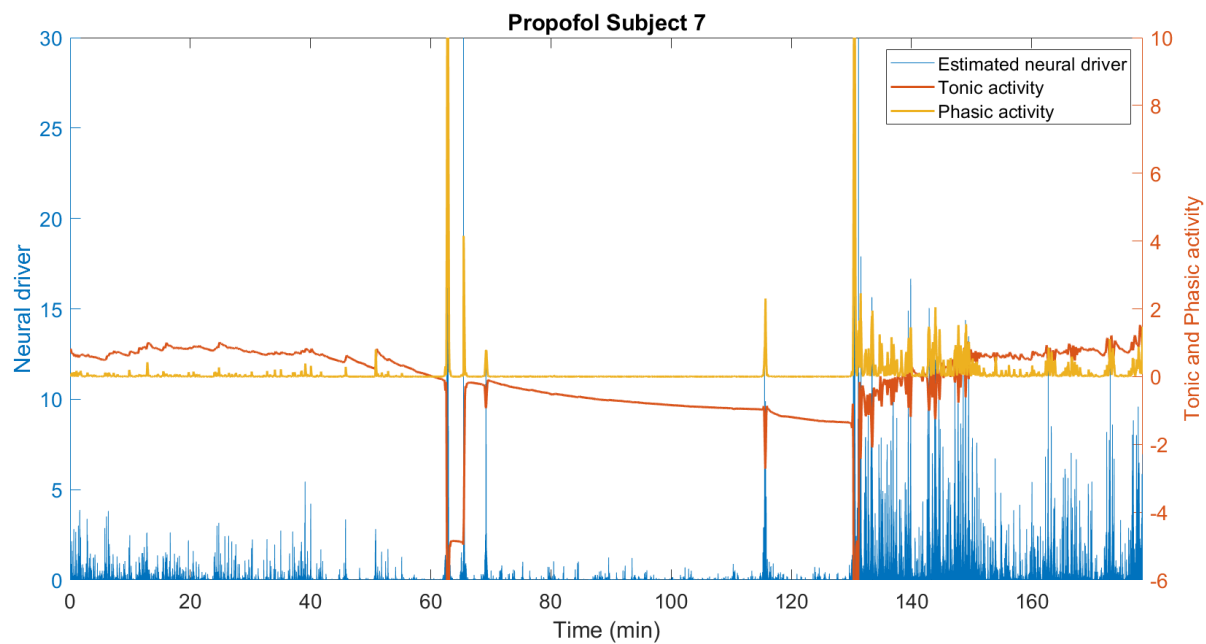


Fig. S44. Results using the cvxEDA algorithm for Subject P7 from the propofol sedation cohort, showing the tonic and phasic components and the estimated neural activity



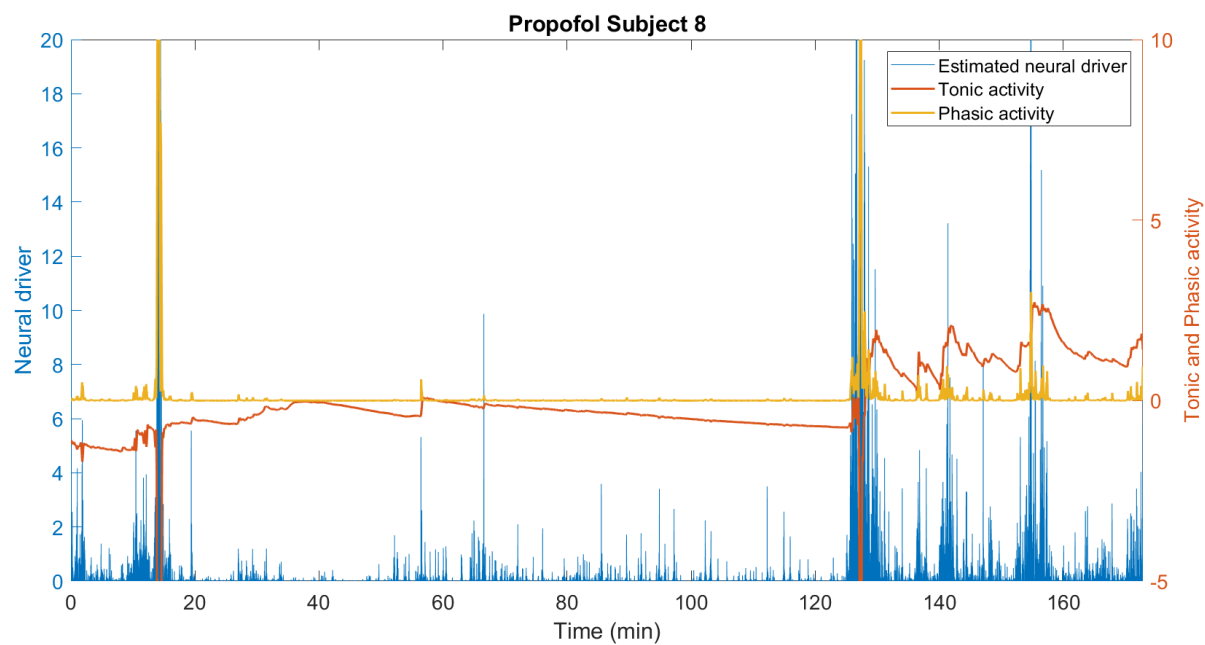


Fig. S45. Results using the cvxEDA algorithm for Subject P8 from the propofol sedation cohort, showing the tonic and phasic components and the estimated neural activity

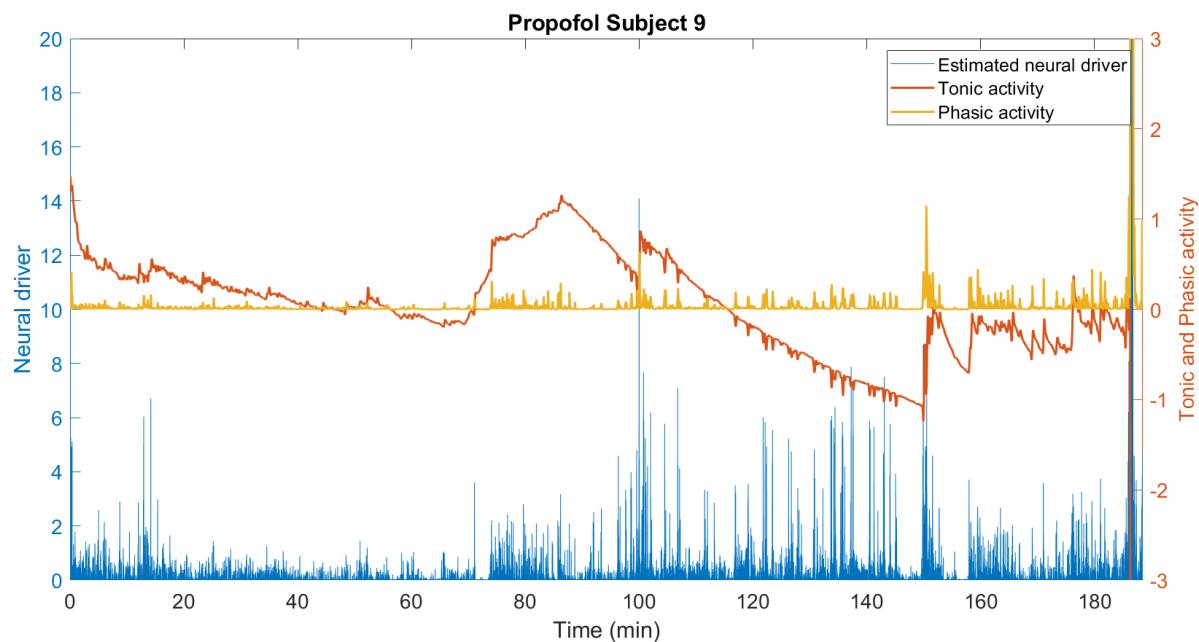


Fig. S46. Results using the cvxEDA algorithm for Subject P9 from the propofol sedation cohort, showing the tonic and phasic components and the estimated neural activity

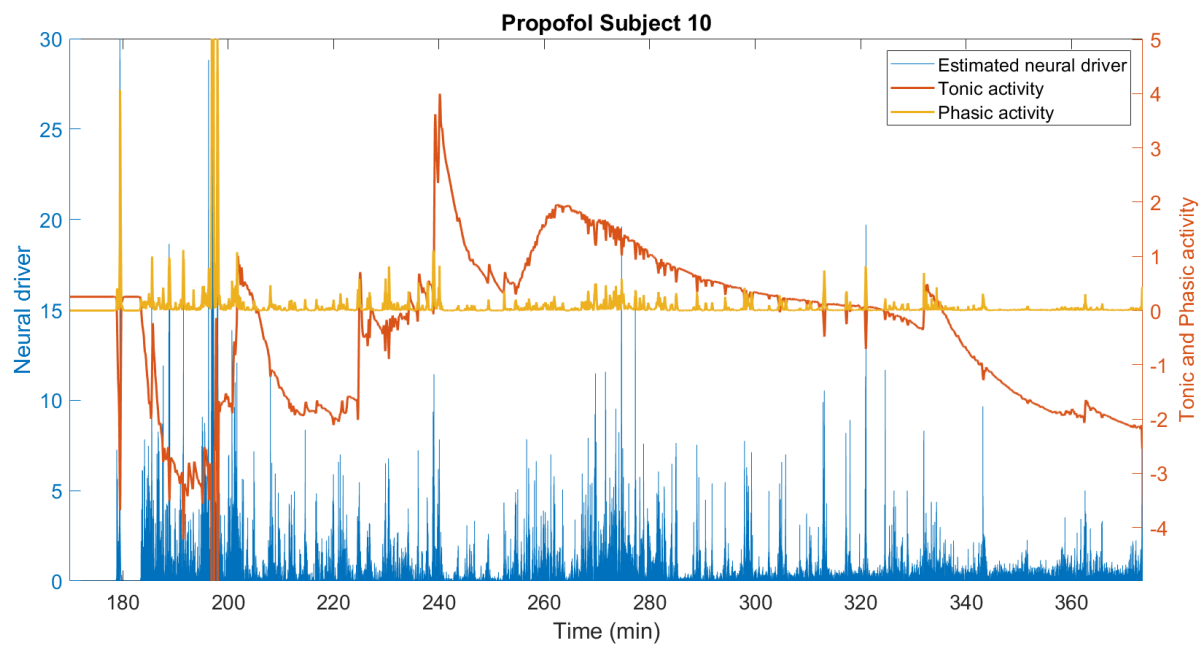


Fig. S47. Results using the cvxEDA algorithm for Subject P10 from the propofol sedation cohort, showing the tonic and phasic components and the estimated neural activity

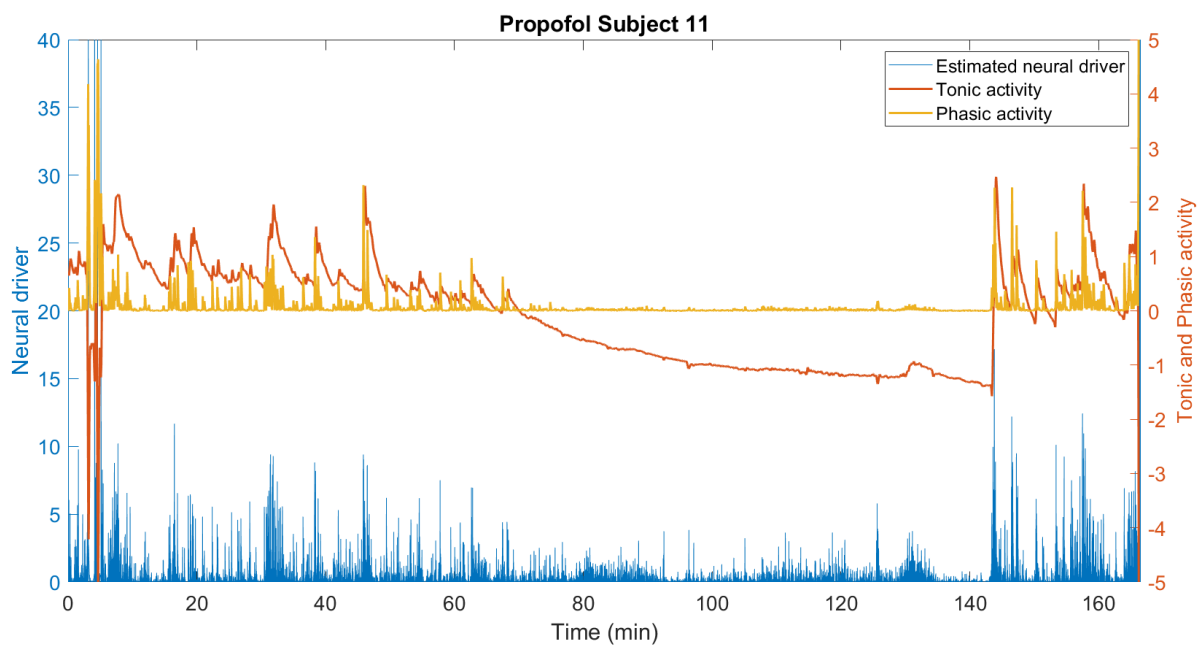


Fig. S48. Results using the cvxEDA algorithm for Subject P11 from the propofol sedation cohort, showing the tonic and phasic components and the estimated neural activity